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# SIMULATING EXPERIMENTAL BREEDER REACTOR II APPROACH-TO-CRITICAL 

by<br>Bilguun Byambadorj

> A dissertation
> submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy in the Department Nuclear Science and Engineering Idaho State University

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## Dedication

I dedicate my dissertation work to my mother, Batkhishig, and father, Byambadorj, for their endless support and encouragement. I also dedicate this work to my beautiful wife, Enkhmaa, and my little brother, Tsenguun.

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#### Abstract

The research presented here focuses on simulating approach-to-critical experiment of Experimental Breeder Reactor II using DIF3D computer code and applying Modified Source Multiplication method.

Historical EBR-II approach-to-critical measured data was obtained from Argonne National Laboratory reports. The dry and wet critical experiment reports include reactor fuel loading configurations, neutron source and detector locations, and count rates of each detector.

Traditional approach-to-critical experiment of EBR-II was simulated, and neutron flux and adjoint flux were calculated by using DIF3D. The MSM correction factor was calculated. The measured 1/M data was corrected.

Finally, the improvement factor (IF) was developed to assist in confirming the improvement from ASM to MSM.


## 1. Introduction

When nuclear reactors startup, the approach-to-critical procedure is used to confirm expected behavior. The critical mass can also be determined by performing an approach-to-critical experiment. Traditionally, the Amplified Source Multiplication (ASM) method was used to predict reactor criticality. The major drawback with the ASM method is that detector efficiency and source importance were assumed to be constant in each fuel loading stage and were not included in the calculation. The Modified Source Multiplication (MSM) method, a better version of ASM, corrects the ASM result by applying source importance and detector efficiency. This research focuses on performing an approach-to-critical simulation of EBR-II using the nodal analysis computer code DIF3D and applying MSM. The research includes a) description of the dry and wet critical experiment of EBR-II, b) development of DIF3D models of EBR-II to simulate the approach-to-critical experiment, c) and development of MSM correction factors.

Before the EBR-II DIF3D model was built, the code needed to be tested for simulation. A simple hexagonal lattice model consisting of uranium fuel and stainless-steel reflector regions was modeled using both DIF3D and KENO VI. The eigenvalue calculation results confirmed DIF3D was successfully compiled and can be used for approach-to-critical simulation.

The EBR-II dry and wet critical experiment models were built by using engineering drawings and "An Integrated Experimental Fast Reactor Nuclear Power Station". ${ }^{1}$ The EBR-II driver assemblies had $48.08 \mathrm{wt} \%$ enriched ${ }^{235} \mathrm{U}$ and blanket assemblies had $0.3 \mathrm{wt} \%$ depleted uranium fuel.

When ASM method is used to predict criticality, the detector efficiency and source strength are assumed to be constant. The ratio of count rates of two consecutive fuel loading stage is calculated as $1 / \mathrm{M}$. The ASM approach-to-critical of EBR-II using measured data was compared to DIF3D simulation. Normalized $1 / \mathrm{M}$ curves show that the DIF3D simulation is close to measured data. More information is provided in Section 5.5.

Every detector in the system predicts different criticality when using ASM method. The MSM method does not assume constant detector efficiency and source strength, and MSM method corrects the ASM critical predictions. With the correction, every detector in the system has closer count rates and predicts consistent criticality. The MSM method and correction factor are discussed in Section 2.2 in more detail. The MSM correction was applied to measured EBR-II approach-to-critical experiment data.

The research results show that using the MSM method is indeed a better choice than ASM method to predict reactor criticality. The improvement factor (IF) was developed to assist in confirming the improvement in the prediction. The MSM predictions of the criticality are more consistent than the ASM predictions according to the IF. The improvement factor will be discussed in Section 6.3 in more detail.

The following sections of this dissertation provide a discussion of the ASM and MSM methodology, a description of EBR-II and a discussion of the EBR-II approach-to-critical experiments. Section 5 provides a chronologically based discussion of the simulation model development that occurred as part of this research project. The chronological development is provided to show the challenges and pitfalls associated with the model development. Results are presented in section 6 including development of a new method IF of evaluating the effectiveness of applying MSM correction factors.

### 1.1 Problem Description

The ASM method assumes detector efficiency and source importance are constant with each fuel addition. However, when performing an approach-to-critical experiment, and when simulating using computer code, the detector efficiency and source importance change with fuel addition. The source importance changes because it is a function of adjoint flux. The adjoint flux changes due to the amount of fuel in the system. The detector efficiency changes because the flux changes due to the amount of fuel in the system.

Monte Carlo method based simulation codes such as MCNP and KENO are not well suited for adjoint flux calculations which is necessary for determining source and detector importance. MCNP does not calculate adjoint flux with a kcode tally. KENO also does not calculate adjoint flux with criticality calculation. The adjoint flux can be calculated in multi-group KENO when calculating k. Also, the importance values can be calculated in KENO and MCNP using the iterated fission probability method which was recently added to both codes. However, these techniques have only been integrated into the codes for use in sensitivity analysis. Modification of the codes to support MSM related calculations requires access to the source code which is typically not provided to non. US. citizens. These issues lead to use of deterministic computer codes such as DIF3D.

DIF3D is an Argonne National Laboratory discrete ordinates and nodal analysis code for both neutron diffusion and transport problems. Additional detail on DIF3D is provided in Section 5.

### 1.2 Background

Every nuclear reactor is started with an approach-to-critical process. The reactor starts in a subcritical configuration with a neutron source present. The reactor slowly approaches a critical configuration as operators add fuel. The process can be simulated by using computer codes such as DIF3D. The ASM method is used to predict the critical configuration. The problem with the ASM method is a lack of inclusion of source importance and detector efficiency. The source importance and detector efficiency change as reactor changes when adding fuel. The MSM method accounts for source importance and detector efficiency changes in the reactor. The MSM method has its own weakness. Pre-calculated source importance and detector efficiency are needed for MSM correction. Fortunately, in a fast neutron spectrum, hexagonal geometry, DIF3D can be used to calculate the source importance and detector efficiency for each configuration. The MSM method is used widely around the world.

Both ASM and MSM methods were used in the French, CEA (Commissariat à l'Energie Atomique) EOLE and MASURCA critical facilities for the determination of reactivity worth by using fission chambers in subcritical configurations. ${ }^{2}$ The standard deviation of the reactivity worth calculated by the MSM method is ten times smaller than the standard deviation of the reactivity worth calculated using the ASM method. These techniques were used to determine the reactivity effect of various perturbations from an unperturbed state. They were based on relative measurements of count rate variations between an unperturbed configuration and a perturbed configuration. The consistency of the MSM calculation and the associated corrections were judged by three indicators: the first indicator addresses the dispersion in inferred reactivities by the ASM when several
detectors are used. The dispersion can be improved when MSM factors are considered. The second indicator addresses the discrepancy between the calculated reactivity and the final MSM-corrected experimental reactivity. The last indicator addresses the calculation-to-experiment discrepancy of the reaction rate ratios between the perturbed configuration and the reference configuration.

In Italy, Imel, G., et al. demonstrated the MSM correction for sensitivity of a TRIGA reactor core. "The TRIGA reactor at the Casaccia Center of ENEA was studied in a number of configurations ranging from $\mathrm{k}_{\text {eff }}$ approximately 0.993 to $0.93{ }^{\prime \prime}{ }^{3}$ A set of experiments were begun not knowing how sensitive the TRIGA reactor would be to core geometry changes, control rod perturbations, etc.

The MSM correction is not necessarily a perfect solution to the source importance and detector efficiency. "The MSM method was tested in calculation of rod worth using an educational reactor in Kyung Hee University, AGN-201K. For this study, a revised nuclear data library and a neutron transport code system, TRANSX-PARTISN, were used for the calculation of correction factors for various control rod positions and source locations". ${ }^{4}$ Experiments were designed and performed to enhance errors in ASM from the location effects of source and detectors. The forward, adjoint, and fixed source fluxes were solved for the MSM correction factor calculation. The maximum difference in correction factors were less than $1 \%$, and therefore, the correction in sub-critical measurement was not done effectively.
"The MSM is applied to the prototype FBR Monju. This static method to estimate the reactivity in sub-critical conditions has already given good results on commercial pressurized water reactors. The MSM consists both in the extraction of the fundamental
mode seen by a detector to avoid the effect of higher modes near sources, and the correction of flux distortion effects due to control rod movement between different reactor states" ${ }^{5}$ Among Monju's unique characters that have an influence on the MSM factors are: the presence of two californium sources near the core and the position of the detector, which is located far from the core outside of the reactor vessel.

The EBR-II dry and wet critical experiments measured results coupled with DIF3D simulation provide a unique source of detailed fast spectrum reactor approach-to-critical measurements where development of MSM correction factors can be determined and evaluated.

### 1.3 Method

To calculate MSM correction factors for a better prediction of EBR-II criticality, a simulation model and measured results are needed. The approach-to-critical experiment will be simulated by DIF3D. The source importance and detector efficiency can be calculated from DIF3D simulation results.

## 2. Subcritical Multiplication

Subcritical multiplication is a theory that represents the changes in the neutron population in a subcritical reactor through reactivity changes. A system is subcritical if, for any nonzero initial neutron population, the expected population, at later times as time goes to infinity, will die out unless it is sustained by either an internal or external neutron source. ${ }^{6}$ If a neutron source is added to the reactor, the neutron population will be both fission neutrons and source neutrons:

$$
\begin{equation*}
N=S+\text { Fission Neutrons } \tag{1}
\end{equation*}
$$

Where:
N - Total number of neutrons in the reactor per generation
$S$ - Number of neutrons from the source
The number of neutrons generated from fission is:

$$
N_{i} * k
$$

Where:
k -Multiplication factor
The total number of neutrons in the next generation according to Equation 1 is:

$$
N_{i+1}=S+N_{i} * k
$$

The total number of neutrons in the $\mathrm{n}^{\text {th }}$ generation will become:

$$
\begin{equation*}
N_{n}=S *\left(1+k+k^{2}+k^{3}+\cdots+k^{n}\right) \tag{2}
\end{equation*}
$$

The subcritical multiplication factor, M , is the factor by which the neutron population increases:

$$
M=1+k+k^{2}+k^{3}+\cdots+k^{n}
$$

When k is greater than $1, \mathrm{M}$ approaches infinity. When k is less than 1 , the subcritical multiplication factor converges to:

$$
\begin{equation*}
M=\frac{1}{1-k} \tag{3}
\end{equation*}
$$

Thus, N will become:

$$
N=\frac{S}{1-k}
$$

When M approaches infinity, k approaches 1 , but $1 / \mathrm{M}$ will approach 0 . Thus, a $1 / \mathrm{M}$ versus fissile mass plot is used when approaching criticality.

### 2.1 Amplified Source Multiplication

Example: Assume there is a neutron source which releases 100 neutrons in each generation and $\mathrm{k}=0.7$ (subcritical). After the first generation, there will be $\mathrm{N} * \mathrm{k}$ fission neutrons in the second generation and the total number of neutrons in particular generation will be represented as Equation 2. In second generation, there will be 100 neutrons from the source and 70 fission neutrons which are produced from fission in first generation. In third generation, there will be 100 neutrons from the source, 70 fission neutrons from second generation which were produced from fission from 100 source neutrons, and 49 fission neutrons from fission of 70 fission neutrons which were produced from first generation. Starting with the $13^{\text {th }}$ generation, the number of neutrons in each generation converges to 330. After few generations, the neutrons in the system will be constant. The total neutron population, fission neutrons and source neutrons in each generation are shown in Table 1.

Table 1. Total Number of Neutrons versus Number of Generations

| Generation | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source neutrons | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| Fission <br> Neutrons |  | 70 | $\begin{aligned} & 70 \\ & 49 \end{aligned}$ | $\begin{aligned} & 70 \\ & 49 \\ & 34 \end{aligned}$ | $\begin{aligned} & 70 \\ & 49 \\ & 34 \\ & 24 \end{aligned}$ | $\begin{array}{\|l\|} \hline 70 \\ 49 \\ 34 \\ 24 \\ 17 \end{array}$ | $\begin{aligned} & 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \end{aligned}$ | $\begin{aligned} & \hline 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \end{aligned}$ | $\begin{aligned} & 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \end{aligned}$ | $\begin{aligned} & \hline 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \\ & 4 \end{aligned}$ | $\begin{aligned} & \hline 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \\ & 4 \\ & 3 \end{aligned}$ | $\begin{aligned} & \hline 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \\ & 4 \\ & 3 \\ & 2 \end{aligned}$ | $\begin{aligned} & \hline 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \\ & 4 \\ & 3 \\ & 2 \\ & 1 \end{aligned}$ | $\begin{aligned} & \hline 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \\ & 4 \\ & 3 \\ & 2 \\ & 1 \\ & 0 \end{aligned}$ | $\begin{aligned} & 70 \\ & 49 \\ & 34 \\ & 24 \\ & 17 \\ & 12 \\ & 8 \\ & 6 \\ & 4 \\ & 3 \\ & 2 \\ & 1 \\ & 0 \end{aligned}$ |
| Total Neutrons | 100 | 170 | 219 | 253 | 277 | 294 | 306 | 314 | 320 | 324 | 327 | 329 | 330 | 330 | 330 |

Since the subcritical multiplication factor (M) and the effective neutron multiplication factor ( $\mathrm{k}_{\text {eff }}$ ) are related, approach to criticality can be performed through monitoring the subcritical multiplication factor. The $\mathrm{k}_{\text {eff }}$ will approach unity as positive reactivity is added to a subcritical reactor. According to Equation 3, as $\mathrm{k}_{\text {eff }}$ gets close to one, the subcritical multiplication factor becomes larger. When the reactor is close to criticality, M increases faster for step insertions of positive reactivity. When the reactor becomes critical, M will be infinite. For this reason, calculating and plotting M during approach to criticality is not possible because $M$ is infinite when the reactor becomes critical. Thus, the inverse of the subcritical multiplication factor $(1 / \mathrm{M})$ is used for plotting and monitoring, since as M approaches to infinity, $1 / \mathrm{M}$ approaches 0 .

The neutron detectors used to monitor the number of neutrons in the core do not count every single neutron in the system. The count rate the detector will see is shown by

## Equation 4.

$$
\begin{equation*}
C R=\eta S \frac{1}{1-k_{e f f}} \tag{4}
\end{equation*}
$$

Where:

$$
\eta \text { - Detector efficiency }
$$

If the detector efficiency and source strength are assumed to be constant from generation to generation, the ratio between two count rates will cancel the detector efficiency and source strength terms.

$$
\begin{equation*}
\frac{C R_{1}}{C R_{2}}=\frac{\eta S \frac{1}{1-k_{1}}}{\eta S \frac{1}{1-k_{2}}}=\frac{M_{1}}{M_{2}} \tag{5}
\end{equation*}
$$

A reference count rate will be needed to simplify the above equation. If $\mathrm{CR}_{1}$ is substituted with the count rate of the initial configuration $\left(\mathrm{CR}_{0}\right)$, then $\mathrm{k}_{0}$ will equal to 0 and $\mathrm{M}_{0}$ will equal to 1 . Thus $1 / \mathrm{M}_{2}$ can be evaluated using count rates as:

$$
\frac{C R_{0}}{C R_{2}}=\frac{1}{M_{2}}
$$

In general:

$$
\begin{equation*}
\frac{C R_{0}}{C R_{i}}=\frac{1}{M_{i}} \tag{6}
\end{equation*}
$$

## Example:

Assume the initial count rate, $\mathrm{CR}_{0}$, is 20 counts per second, along with count rates as a function of control rod position as shown in Table 2.

Table 2. Count Rates in each Control Rod Position

| Rod Position <br> (inches) | Count Rates <br> $(\mathrm{cps})$ |
| :--- | :--- |
| 1 | 22 |
| 3 | 27 |
| 5 | 33 |
| 7 | 39 |
| 9 | 54 |
| 11 | 94 |
| 15 | 200 |

The $1 / \mathrm{M}$ values calculated for each rod position are listed in Table 3.
Table 3. Calculated 1/M Value

| Rod Position <br> (inches) | Count Rate <br> $(\mathrm{cps})$ | $1 / \mathrm{M}$ |
| :--- | :--- | :--- |
| 0 | 20 | 1 |
| 1 | 22 | 0.909 |
| 3 | 27 | 0.741 |
| 5 | 33 | 0.606 |
| 7 | 39 | 0.513 |
| 9 | 54 | 0.370 |
| 11 | 94 | 0.213 |
| 15 | 200 | 0.100 |

The values in Table 3 can be plotted as shown in Figure 1 with $1 / \mathrm{M}$ in the y -axis and rod position in the $x$-axis. The x-intercept of the extrapolation between two consecutive points is the prediction of criticality.


Figure 1 . The $1 / \mathrm{M}$ value as a function of control rod position.

The extrapolation of the last pair of points is more accurate than that of the previous pairs because the $1 / \mathrm{M}$ values of the last two points are close to 0 and reactor is close to criticality. It is shown that the system will go critical when control rod position reaches 18.5 inches. "The general rule of thumb for adding more fuel during approach-to-critical is to add no more than half of the additional amount of fuel needed to achieve criticality with the control rods in the least reactive position. For example, if $1 / \mathrm{M}$ curve predicts that reactor needs 6 more fuel assemblies to achieve criticality with the control rods in the least reactive position, operator should add no more than 3 fuel assemblies, and then take the count rate."

The ASM method can be used for either adding more fuel assemblies or moving the control rods in the system. Nuclear reactor approach-to-critical experiments do not actually start with no fuel in the core when $\mathrm{k}^{-}$eff $=0$. In fact, it starts with a subcritical configuration where $\mathrm{k}_{\text {eff }}>0$. Also, simulating approach-to-critical with $\mathrm{k}_{\text {eff }}=0$ is a very poor choice,
because the $\mathrm{k}=0$ has no physical or mathematical meaning. A better approach is a starting point with a significant $\mathrm{k}(>0.9)$.

### 2.2 Modified Source Multiplication

The detector efficiency and source importance is not always constant during approach-to-critical, in fact, they are different with each new core configuration. The detector efficiency is a ratio of detected neutrons and total neutrons in the system. The total number of neutrons in the system is a fixed value established by the source and M . The detectors only count those neutrons which interact with the detector. Thus, the number of neutrons detected is always much smaller than the total number of neutrons.

Assume a system consists of fuel assemblies, three detectors and a source as shown in Figure 2.


Figure 2. A hexagonal lattice fuel configuration with neutron source and detectors
(Pink is fuel and teal is sodium).

In this system, detector \#1 and \#3 have the same efficiency based on symmetry.
Detector \#2 will have different efficiency due to its location in relation to the source.
Now, we add fuel on one side of the core region as shown in Figure 3. The detectors \#1 and \#3 will no longer have equal efficiency due to the added fuel. The number of fission neutrons counted in detector \#1 and \#3 will be different. Similarly, detector \#2 will experience an altered efficiency due to the core configuration change. The source importance will also change due to change in fission neutrons and adjoint flux.


Figure 3. A hypothetical model with added fuel assemblies.

Now we have 3 detectors each with different counts but the total neutron population is the same for all. Thus, the efficiency is different between detectors and also different from prior configurations.

In this case, equation 5 cannot be used to eliminate detector efficiency and source strength. Thus, we have the following equation:

$$
\begin{equation*}
\frac{C R_{1}}{C R_{2}}=\frac{\eta_{1} S_{1} \frac{1}{1-k_{1}}}{\eta_{2} S_{2} \frac{1}{1-k_{2}}}=\frac{\eta_{1} S_{1}\left(1-k_{2}\right)}{\eta_{2} S_{2}\left(1-k_{1}\right)}=\frac{\eta_{1} S_{1} M_{1}}{\eta_{2} S_{2} M_{2}} \tag{7}
\end{equation*}
$$

The modified source multiplication (MSM) factor is the change in the $\eta \mathrm{S}$ term between two states. To obtain the physical meaning, these terms need to be mathematically defined.

$$
\begin{equation*}
\eta=\frac{\text { Detected Neutrons }}{\text { Total Number of Neutrons }}=\frac{\int \Sigma_{d} \phi}{\int v \Sigma_{f} \phi}=\frac{\left\langle\Sigma_{d} \phi\right\rangle}{\langle F \phi\rangle} \tag{8}
\end{equation*}
$$

Where:

$$
\Sigma_{d}-\text { Detector Cross Section }
$$

As shown in equation 8, the symbol of inner product, <>>, means the integral over all the reactor space and energy. A new term, source importance, needs to be defined using the adjoint flux $\phi^{*}$ :

$$
\begin{equation*}
\text { Source Importance }=\frac{\text { Average Source Neutrons }}{\text { Fission Neutrons }}=\frac{\left\langle\phi^{*} S\right\rangle}{\left\langle\phi^{*} F \phi\right\rangle} \tag{9}
\end{equation*}
$$

The "effective" source neutrons can be represented by multiplying source importance by total fission neutron rate:

$$
\begin{equation*}
S_{e f f}=\frac{\left\langle\phi^{*} S\right\rangle}{\left\langle\phi^{*} F \phi\right\rangle}\langle F \phi\rangle \tag{10}
\end{equation*}
$$

The MSM correction factor can be found by multiplying efficiency by the effective source term:

$$
\begin{equation*}
\eta S_{e f f}=\frac{\left\langle\phi^{*} S\right\rangle}{\left\langle\phi^{*} \mathrm{~F} \phi\right\rangle}\langle\mathrm{F} \phi\rangle \frac{\left\langle\Sigma_{d} \phi\right\rangle}{\langle\mathrm{F} \phi\rangle}=\frac{\left\langle\phi^{*} S\right\rangle}{\left\langle\phi^{*} \mathrm{~F} \phi\right\rangle}\left\langle\Sigma_{d} \phi\right\rangle \tag{11}
\end{equation*}
$$

The adjoint flux at position $r$ is a measure of how effective an absorber inserted at position $r$ in the reactor is in changing the reactivity of the core. It means the adjoint flux is the "importance" of the point r with respect to reactivity changes. It is not limited to only absorbers in the reactor.

The application of the MSM correction factors is discussed in Section 6.

## 3. Detailed Description of EBR-II

The Experimental Breeder Reactor II (EBR-II) was a sodium cooled, fast spectrum, breeder reactor. It had a maximum thermal output of 62.5 MW and produced approximately

20 MWe . The EBR-II power plant complex was located in Idaho, and the plant included a complete, remotely-operated fuel-processing and fuel-element fabrication facility. It was the first reactor in the US to operate on a closed fuel cycle.

The EBR-II reactor core consisted of 637 hexagonal assemblies. The assemblies were divided into three regions: core, inner blanket, and outer blanket. Later, the core was reconfigured to support irradiation activities. As shown in Figure 4, the control rods were located at the outer edge of the core region and two safety rods were located at the third row of the core region.


Figure 4. The EBR-II reactor core configuration.
The approach-to-critical experiments core used for this analysis consisted of two safety rods, 11 regular control rods, one special control rod, 47 driver subassemblies, 66 inner blanket subassemblies and 510 outer blanket subassemblies.

### 3.1 Driver Subassembly

The driver subassembly, as shown in Figure 5, consisted of three regions containing fissile materials: upper blanket, driver, and lower blanket region. The over-all length of the driver subassembly was $233.24-\mathrm{cm}$. The fuel region consists of 91 fuel elements in a hexagonal lattice.


Figure 5. Driver fuel subassembly (all dimensions are in inches).

An individual fuel element, as shown in Figure 6, was $44.07-\mathrm{cm}$ long not including spade in the bottom. The fuel element consisted of fuel slug, sodium gap, stainless-steel 316 cladding, stainless-steel 316 cap and stainless-steel 316 wire wrap. The report "The EBR-II Dry Critical Experiments Experimental Results" indicate that the fresh fuel slug was $95 \mathrm{wt} \%$ uranium and $5 \mathrm{wt} \%$ fissium alloy. ${ }^{7}$ Fissium is a given name to a mixture of fission product elements (atomic numbers 40 to 47) as shown in Table 4. The uranium is $48.08 \%$ enriched ${ }^{235} \mathrm{U}$. The active fuel region was $36.12-\mathrm{cm}$ long, and fuel slug diameter was $0.366-\mathrm{cm}$.


Figure 6. Driver fuel element (all dimensions are in inches).

Table 4. Uranium-Fissium Alloy Composition

| Elements | Weight \% |
| :--- | ---: |
| Uranium | 95.00 |
| Molybdenum | 2.46 |
| Ruthenium | 1.96 |
| Palladium | 0.19 |
| Zirconium | 0.10 |
| Niobium | 0.01 |

The upper and lower blanket regions were geometrically identical to each other. Both consisted of 19 pin-type elements in a hexagonal lattice. The blanket elements, as shown in Figure 7, were about 3.78 inches longer and had 2.2 times bigger diameter than a fuel element. It consisted of stainless-steel 316 cladding, depleted uranium, sodium gap, and stainless-steel 316 plug springs. The blanket slug, $0.3 \%$ depleted uranium, was $45.72-\mathrm{cm}$ in length and $0.803-\mathrm{cm}$ in diameter.


Figure 7. Upper and lower blanket element (all dimensions are in inches).

### 3.2 Control Subassembly

Each EBR-II control rod had its own electrical-mechanical drive mechanism. There were 11 control rods and one special control rod during critical experiments. The control rods were arranged that one drive mechanism operates at any given time except reactor scram when all 12 drive mechanisms operate together. Each control rod moved 14 inches $(35.56 \mathrm{~cm})$ vertically with a constant speed. Control rods were disconnected from their drive mechanisms, when they were in the least reactive position, during fuel handling operations. Figure 8 shows the control rod motion. The control assembly consisted of two hexagonal tubes. The smaller one contains the fuel elements and fits into a normal driver size hexagonal tube. When the control rod is moved up by 14 inches, the fuel section of the control rod is 0.25 inches $(0.635 \mathrm{~cm})$ below the driver fuel region. When a control rod is at the least reactive position, the top of the control rod fuel section is aligned with the bottom of the driver fuel section.

The control rod fuel section consists of 61 fuel elements in a hexagonal lattice. The fuel element is a standard driver fuel element which consists of $90 \mathrm{wt} \%$ uranium and $10 \mathrm{wt} \%$ fissium fuel slug, stainless-steel 316 cladding, wire-wrap and end plug.

Since the control rods are fuel, they are inserted into the core to add reactivity and lowered below the core region to remove reactivity. This is different than poison control rods used in LWR's.


Figure 8. Control rod (all dimensions are in inches).

Above the fuel section, there is a void and upper reflector section. It is different for the one special control rod. These sections of the special control rod had $\mathrm{B}_{4} \mathrm{C}$ poison elements. There were 7 poison elements in the special control rod in a triangular lattice. As shown in Figure 9, the capsule contains $\mathrm{B}_{4} \mathrm{C}$ poison and a stainless-steel shield. The upper reflector section of a regular control rod consists of stainless-steel reflector. The special control rod contains $\mathrm{B}_{4} \mathrm{C}$ poison capsules instead of stainless-steel reflector.


Figure 9. $\mathrm{B}_{4} \mathrm{C}$ capsule (all dimensions are in inches).

### 3.3 Safety Subassembly

The EBR-II safety subassemblies consisted of a safety rod and guide thimble. In certain ways, the safety rods were almost identical to control rods, except the length of the void section and the design of the lower end, as shown in Figure 10. The safety rod drive system is below the reactor core; thus, it would not interfere with fuel loading or control rod mechanisms which are on the top of the reactor. Both safety rods were fully inserted into the reactor, at the most reactive position, during normal reactor operations and fuel handling. The two safety rods were moved together with a single drive mechanism. The purpose of the safety rod was to shut down the reactor from unintended critical condition during refueling.


Figure 10. Safety rod.

### 3.4 Inner and Outer Blanket

As shown in Figure 11, the inner and outer blanket subassemblies consisted of 19 depleted uranium fuel elements in triangular lattice, a bottom adapter, and an upper pole piece. The only difference between inner and outer blanket subassemblies was the bottom adapter and the coolant flow design as shown in Figure 12.

The blanket elements were about 3.6 times longer and 2.5 times larger diameter than the driver fuel elements. Each blanket element was $158.59-\mathrm{cm}$ long, and $1.1-\mathrm{cm}$ in diameter. The blanket element consisted of five fuel pins each $27.94-\mathrm{cm}$ long, sodium gap, stainless-steel 316 spring, bottom end spade and top end cap. The depleted uranium fuel consisted of $0.3 \mathrm{wt} \%{ }^{235} \mathrm{U}$ and $99.7 \mathrm{wt} \%{ }^{238} \mathrm{U}$.



Inner Blanket Subassembly Bottom Adapter


Outer Blanket Subassembly Bottom Adapter

Figure 11. Inner and outer blanket subassemblies (all dimensions are in inches).


Figure 12. Inner and outer blanket subassembly cross-sectional view (all dimensions are in inches).

## 4. EBR-II Critical Experiment

The approach-to-critical experiments of EBR-II were zero power experiments. According to "EBR-II Dry Critical Experiments Experimental Program, Experimental Procedures and Safety Consideration" ${ }^{8}$ report, there were two objectives to these experiments:

1. To determine information relating to the performance of the system without sodium coolant, for future comparison with information derived with sodium coolant. By comparison, it will then be possible to ascertain various sodium effects on the neutronics of the system.
2. To determine and/or verify certain operational data to permit modification or improvement of the system (neutron shield, instrumentation, etc.) prior to the introduction of sodium into the system. After sodium filling it will be difficult to alter, modify, or correct many of the system components.

There were some significant considerations regarding the experiment such as a) the maximum reactor power level should be less than $1 \mathrm{~kW}, \mathrm{~b}$ ) there should not be any initial contamination of the fissionable or fertile materials with fission products or plutonium, with no significant quantities of these material generated during critical experiments, and c) the dry critical reactor mass is larger than wet critical reactor mass, so the core must be at least $20 \%$ larger in diameter than it is considered for the reactor with sodium present.

### 4.1 Dry Critical Experiment

The EBR-II reactor achieved dry criticality on September 30, 1961. The reactor started up with no sodium coolant in the vessel. The experiment used the same components and fuel as normal power operations. This operation was simplified due to low power level
( $<1 \mathrm{~kW}$ ). Since the reactor did not have liquid sodium coolant, special in-core instruments were used to obtain more accurate information of the core during operation.

Since the dry critical mass of ${ }^{235} \mathrm{U}$ was 47.9 kg larger than wet critical mass, additional 17 enriched subassemblies were needed. These enriched subassemblies were loaded in the inner blanket region. However, there was no specific engineering drawings of the enriched inner blanket subassembly. It was mentioned in the "EBR-II Dry Critical Experiments" ${ }^{8}$ report that there were indeed inner blanket subassemblies which were highly enriched. The ${ }^{235} \mathrm{U}$ amount was equal to that of a driver subassembly.

Prior to the critical experiment, the core was loaded with stainless-steel dummy subassemblies, natural uranium subassemblies, inner and outer blanket subassemblies. The approach-to-critical experiment was started with the two safety rods inserted into their most reactive positions, all control rods were inserted in their least reactive positions and one driver subassembly was at the center location as shown in Figure 13. An antimony-124 beryllium neutron source rod was located in $7^{\text {th }}$ row. The source strength was 270 Ci and a half-life of 60 days. During the critical experiment, the source strength decayed 13\%, and all count rates were corrected to 189 Ci source strength.

In a dry critical experiment, it was possible to use in-core neutron detectors. $\mathrm{BF}_{3}$ neutron detectors were located in inner blanket row 6 and 7, and outer blanket row 11 and 13.


Figure 13. Dry critical experiment, approach-to-critical loading \#1.

From this point on, driver and enriched inner blanket subassemblies were added to the core as symmetric as possible. The core configurations are shown in Figure 14 and Figure 15. Since EBR-II subassemblies were only locked at the bottom, a single subassembly was allowed to be removed during fuel loading.


Figure 14. Dry critical experiment, approach-to-critical loading \#2-\#7.


Figure 15. Dry critical experiment, approach-to-critical loading \#8 - \#11.
The amount of ${ }^{235} \mathrm{U}$ loaded into the core is shown in Table 5.

Table 5. Dry Critical Experiment Fuel Subassembly Loading Increment

| Loading No. | Number of <br> Subassemblies <br> Added/Loading | Total Number of <br> Subassemblies | Total Kg <br> of ${ }^{235} \mathrm{U}$ |
| :---: | :---: | :---: | ---: |
| 1 | 15 | 15 | 29.21 |
| 2 | 16 | 31 | 74.18 |
| 3 | 9 | 40 | 99.49 |
| 4 | 9 | 49 | 124.98 |
| 5 | 6 | 55 | 141.86 |
| 6 | 6 | 61 | 158.81 |
| 7 | 6 | 67 | 175.73 |
| 8 | 6 | 73 | 192.67 |
| 9 | 4 | 77 | 203.95 |
| 10 | 6 | 83 | 220.88 |
| 11 | 4 | 87 | 232.18 |

### 4.2 Wet Critical Experiment

The wet critical experiments were performed after various dry critical experiments. ${ }^{9}$ The reactor was filled by liquid sodium coolant and similar low-power experiments were performed. These experiments were designed to provide two types of information: a) the data that are necessary for operating power reactor system such as control rod worth, nuclear instrument response and neutron source strength, and b) the general information such as total worth of the sodium coolant and critical size of the reactor. The wet critical experiments were performed at $600^{\circ} \mathrm{F}$.

Although, the dry and wet critical experiments were similar, there were some differences such as core loading, neutron source strength and location, and detector locations. As shown in Figure 16, the neutron detectors were located in thimbles J1, J2 and J3. There were five detectors total; three fission and two $\mathrm{BF}_{3}$ detectors. Two of the fission detectors were in J 1 thimble, one fission and one $\mathrm{BF}_{3}$ detectors were in J 2 thimble, and one
$\mathrm{BF}_{3}$ detector was in J 3 thimble. There were three antimony-beryllium neutron sources located in subassemblies in row 7 and 8.

The core was filled with dummy driver, natural uranium driver, inner and outer blanket subassemblies before the critical experiment. The core loading started with loading two safety rods and 12 control rods containing total of 26.5 kg of ${ }^{235} \mathrm{U}$. Then the three neutron sources were loaded in reactor locations 8-E-2, 7-E-3 and 7-E-5.


Figure 16. The EBR-II wet critical experiment core before loading fuel.

The counts were taken with all control rods up and down positions. The fuel loading increments and amount of ${ }^{235} \mathrm{U}$ are listed in Table 6.

Table 6. Wet Critical Experiment Fuel Subassembly Loading Increment

| Loading No. | Number of <br> Subassemblies <br> Added/Loading | Total Number of <br> Subassemblies | Total Kg <br> of ${ }^{235} \mathrm{U}$ |
| :---: | :---: | :---: | ---: |
| 1 | 14 | 14 | 26.50 |
| 2 | 17 | 31 | 74.28 |
| 3 | 6 | 37 | 91.09 |
| 4 | 6 | 43 | 108.04 |
| 5 | 6 | 49 | 124.96 |
| 6 | 6 | 55 | 141.93 |
| 7 | 5 | 60 | 155.99 |
| 8 | 4 | 64 | 167.29 |
| 9 | 3 | 67 | 175.79 |
| 10 | 3 | 70 | 184.29 |

The Figure 17 shows the wet critical fuel loading diagram. As shown in Table 6, the loading \#1 (first column) has total of 14 subassemblies (third column). The subassemblies \#1 to \#14 in Figure 17 will be loaded. The loading \#2 has total of 31 subassemblies. The subassemblies \#15 to \#31 will be added to the previous configuration.


Figure 17. The wet critical experiment fuel loading diagram.

## 5. Benchmark Simulation Model

Deterministic reactor physics simulation codes such as DIF3D solve the Boltzmann transport equation using multi-group and finite difference methods.

The DIF3D VARIANT (VARIational Anisotropic Neutron Transport) code performs nodal neutron transport calculations using $\mathrm{P}_{\mathrm{N}}$ theory in Cartesian and hexagonal two- and three-dimensional geometries. ${ }^{10}$ It starts with the time independent form of Boltzmann transport equation:

$$
\begin{align*}
& \hat{\Omega} \cdot \vec{\nabla} \Phi(\vec{r}, \widehat{\Omega}, E)+\Sigma_{t}(\vec{r}, E) \Phi(\vec{r}, \hat{\Omega}, E)= \\
= & \iint \Sigma_{s}\left(\vec{r}, \hat{\Omega}^{\prime} \rightarrow \hat{\Omega}, E^{\prime} \rightarrow E\right) \Phi\left(\vec{r}, \hat{\Omega}^{\prime}, E^{\prime}\right) d \hat{\Omega}^{\prime} d E^{\prime}  \tag{12}\\
+ & S(\vec{r}, \widehat{\Omega}, E)
\end{align*}
$$

Where:
$\Phi(\vec{r}, \widehat{\Omega}, E)$ - neutron angular flux
$\Sigma_{t}(\vec{r}, E)$ - sum of all possible neutron reaction probabilities with energy E at the point $\vec{r}$ $\Sigma_{s}\left(\vec{r}, \widehat{\Omega}^{\prime} \rightarrow \widehat{\Omega}, E^{\prime} \rightarrow E\right)$ - probability that a particle at $\vec{r}$ with energy E' traveling in the direction $\widehat{\Omega}^{\prime}$ is scattered into energy dE about E with direction $d \widehat{\Omega}$ about $\widehat{\Omega}$ $S(\vec{r}, \widehat{\Omega}, E)$ - generic neutron source that includes fission, fixed and external sources.

The first step of solving the Boltzmann transport equation is discretizing space and energy as shown in Figure 18. The multi-group approach divides the energy range into G intervals with upper and lower energy cutoff at $\mathrm{E}_{0}$ and $\mathrm{E}_{\mathrm{G}}$ as shown below.


Figure 18. The splitting of the energy range into energy groups.

After applying the multi-group approach to the angular flux and source and cross sections, equation 12 becomes:

$$
\begin{align*}
& \hat{\Omega} \cdot \vec{\nabla} \Phi_{g}(\vec{r}, \hat{\Omega})+\Sigma_{t, g}(\vec{r}) \Phi_{g}(\vec{r}, \widehat{\Omega})= \\
& \sum_{g^{\prime}=1}^{G} \Sigma_{s, g^{\prime} \rightarrow g}(\vec{r}) \varphi_{g}(\vec{r})+S_{g}(\vec{r}, \widehat{\Omega}) \quad \mathrm{g}=1 . . \mathrm{G} \tag{13}
\end{align*}
$$

Where the scalar flux is:

$$
\begin{equation*}
\varphi(\vec{r})=\int \Phi(\stackrel{\rightharpoonup}{r}, \widehat{\Omega}) d \Omega \tag{14}
\end{equation*}
$$

The first term of the Equation 13 is in derivative form. This can be simplified by the difference in a small mesh interval. The entire problem geometry can be dived into mesh intervals as shown in Figure 19. The neutron flux can then be solved at every mesh point.


Figure 19. Spacial mesh interval.

The differential term can be represented as a finite difference:

$$
\begin{equation*}
\left.\frac{\delta \Phi(\vec{r}, \widehat{\Omega})}{\delta x}\right|_{x_{k}} \approx \frac{\Phi_{k+1}-\Phi_{k-1}}{x_{k+1}-x_{k-1}} \tag{15}
\end{equation*}
$$

Thus,

$$
\begin{equation*}
\Phi_{k}=\frac{\Phi_{k+1}-\Phi_{k-1}}{2} \tag{16}
\end{equation*}
$$

Similarly, the angular dependence can be discretized and the Boltzmann transport equation can be solved numerically using DIF3D.

### 5.1 DIF3D Neutron Cross-Section Confirmation

Before simulating a nuclear reactor, the simulation tool must be confirmed to be working properly. A DIF3D model and using Argonne National Laboratory supplied neutron cross-section data was compared with a $\mathrm{KENO} \mathrm{VI}^{11}$ model. The problem specific cross-sections are generated by MC ${ }^{2} .{ }^{12}$ The EBR-II specific cross-section file was acquired from Argonne National Laboratory. This cross-section file was specific for hexagonal geometry simulations.

A simple critical model using a hexagonal lattice was built using both KENO VI and DIF3D. The model, as shown in Figure 20, was used for comparing the cross-sections and confirming DIF3D installation and execution. This model consisted of two regions; fuel region and stainless-steel reflector. For simplicity's sake, the stainless steel consisted of $12 \% \mathrm{Ni}, 17 \% \mathrm{Cr}$, and $71 \% \mathrm{Fe}$. The fuel region consisted of $48.86 \%$ enriched ${ }^{235} \mathrm{U}$. The initial model started with fuel region only. The initial composition was started with $50 \%$ enriched ${ }^{235} \mathrm{U}$ which produced $\mathrm{k}_{\text {eff }}=1.000$ on KENO VI. On the other hand, the $\mathrm{k}_{\mathrm{eff}}$ of an identical model on DIF3D was about 0.8. The fuel region was surrounded by stainless-steel
reflector to reduce leakage. As reflectors being added, the $\mathrm{k}_{\text {eff }}$ from DIF3D increased significantly. But, the $\mathrm{k}_{\text {eff }}$ from KENO VI increased slightly. The ${ }^{235} \mathrm{U}$ atom density was slowly reduced to $48.86 \%$ enriched ${ }^{235} \mathrm{U}$ to make the model critical on KENO VI as reflectors kept being added.


Figure 20. A simple hexagonal lattice for confirmation, pink is fuel, teal is stainless steel.

A simple hexagonal assembly consisting of a homogenized mixture of ${ }^{235} \mathrm{U},{ }^{238} \mathrm{U}$ and Na was used as a fuel assembly. The fuel region was surrounded by sodium and a stainless-steel reflector. The stainless-steel above and below sodium were 70 cm long. There were 7 rows ( 127 hexagons) of fuel assemblies in the model. The fuel assemblies are surrounded by 31 rows of stainless steel reflector to reduce leakage. Table 7 shows the effective multiplication factor was calculated using both KENO VI and DIF3D.

Table 7. $\mathrm{K}_{\text {eff }}$ Calculated from both KENO VI and DIF3D

| Code | $\mathrm{k}_{\text {eff }}$ | Uncertainty |
| :--- | :--- | :--- |
| KENO VI | 1.00021 | $\pm 0.0003$ |
| DIF3D | 0.99909 |  |

In the KENO VI model, ENDF-v7 continuous energy cross section data was used. The model was run with 250 generations and 10,000 neutrons per generation. The first 50 generations were skipped to ensure convergence. On the other hand, the DIF3D model was run with 33 group specific cross-section data of EBR-II. The $8^{\text {th }}$ order of the polynomial approximation of the source within the node, the $8^{\text {th }}$ order of the polynomial approximation of the fluxes within the node, and the second order of the polynomial approximation of the leakage on the surfaces of the nodes were used. The $\mathrm{P}_{3}$ flux and leakage expansions were selected.

The $\mathrm{k}_{\text {eff }}$ values from KENO VI and DIF3D confirm that DIF3D and EBR-II specific cross-section data can be used for simulation. Also, the DIF3D was compiled and executed properly.

### 5.2 DIF3D Model Development

Due to geometric limitations of DIF3D, the EBR-II model was homogenized. To be consistent with the physical subassemblies, each subassembly was divided into sections and then homogenized. The driver fuel subassembly was divided into 10 sections as shown in Figure 21. Sodium and stainless-steel pieces were added on the top and the bottom of the driver subassembly. Another DIF3D geometry limitation is that every subassembly must have the same height. The sodium region was added above and below each subassembly including safeties, inner and outer blanket to compensate for the motion of control rods. The list of material composition of the driver fuel subassembly is shown in Table 8.


Figure 21. Homogenized driver fuel subassembly.

Table 8. Material Composition of Homogenized Driver Fuel Subassembly
(units in grams)

|  | $\begin{aligned} & \text { Above Upper Blanket } \\ & \text { Fuel Region } \end{aligned}$ |  |  |  | 0 0.0 0 0 0 0 0 0 0 0 0 0 0 |  |  |  | Lower Blanket Spade and -bar grid |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{235} \mathrm{U}$ |  | 23.43 |  |  | 2807.79 |  |  | 23.43 |  |  |
| ${ }^{238} \mathrm{U}$ |  | 7787.90 |  |  | 3032.04 |  |  | 7787.90 |  |  |
| Fs* |  |  |  |  | 307.36 |  |  |  |  |  |
| Na | 292.36 | 645.78 | 42..83 | 108.25 | 462.29 | 23.41 | 109.66 | 645.78 | 54.19 | 1410.58 |
| Fe | 131.73 | 1254.78 | 261.47 | 653.90 | 1196.63 | 172.14 | 669.42 | 1254.74 | 771.81 | 8610.62 |
| Ni | 22.26 | 212.08 | 44.19 | 110.52 | 202.25 | 29.09 | 113.14 | 212.08 | 130.45 | 1455.32 |
| Cr | 31.54 | 300.44 | $62 . .61$ | 156.57 | 286.52 | 41.22 | 160.29 | 300.44 | 184.80 | 2061.70 |

Fs* is a shortcut of fissium.
Neutron leakage in a small reactor like EBR-II is significant. For example, "the neutron flux of a bare spherical reactor of 50 cm is given by $\varphi=5 * 10^{13} * \frac{\sin (0.0628 r)}{r}$ neutrons $/ \mathrm{cm}^{2}$-sec, where r is measured from the center of the reactor". ${ }^{13}$ The number of neutrons escaping from this reactor is equal to $1.58 * 10^{15}$ neutrons $/ \mathrm{sec}$. DIF3D could not solve problems with significant leakage due to application of boundary conditions in the hexagonal lattice geometry. To decrease the leakage, $60-\mathrm{cm}$ long stainless-steel reflectors were added at the top and bottom of the EBR-II model and 9 rows of stainless-steel reflectors were placed around the core.

The inner and outer blanket subassemblies in the model were geometrically identical. As shown in Figure 22, the blanket subassembly is divided into five pieces: lower adapter, spade and t-bar grid, blanket fuel region, above blanket fuel region and top plug and then homogenized.


Figure 22. Homogenized blanket fuel subassembly.

The detailed material description of homogenized subassembly is listed in Table 9.
Table 9. Material Composition of Homogenized Driver Fuel Subassembly (units in grams)

|  | $\begin{aligned} & \frac{000}{\stackrel{1}{2}} \\ & \stackrel{n}{0} \end{aligned}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{235} \mathrm{U}$ |  |  | 94.31 |  |  |
| ${ }^{238} \mathrm{U}$ |  |  | 47060.36 |  |  |
| Na | 38.08 | 126.73 | 760.39 | 54.19 | 1410.58 |
| Fe | 542.43 | 981.97 | 4190.80 | 771.81 | 8610.62 |
| Ni | 91.68 | 165.97 | 708.30 | 130.45 | 1455.32 |
| Cr | 129.88 | 235.12 | 1003.43 | 184.80 | 2061.70 |

Since the safety and the control rods were identical, the same geometrical model was used for both. The only difference between a regular control rod and the safety rod is the length of the lower adapter and the region above the upper reflector. In the homogenized model of safety and control rods, these regions have equal volume but different atom densities. Figure 23 shows the homogenized control and safety subassemblies. The material compositions of the homogenized safety and control rods are shown Table 10.


Figure 23. Homogenized control and safety subassemblies.

Table 10. Material Composition of Homogenized Control and Safety Subassembly (units in grams)

| $\begin{aligned} & \frac{0}{\tilde{E}} \\ & \stackrel{y}{\tilde{y}} \\ & \sum \end{aligned}$ | $\begin{aligned} & \ddot{0} \\ & 0.0 \\ & \stackrel{0}{0} 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | $\begin{aligned} & .0 \\ & \cdot 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  | .0 00 0 0 0 0 0 0 0 0 0 0 |  | $\begin{gathered} \text { Lower Reflector and } \\ \text { Adapter } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{235} \mathrm{U}$ |  |  |  |  | 1882.14 |  |  |
| ${ }^{238} \mathrm{U}$ |  |  |  |  | 2032.46 |  |  |
| Fs* |  |  |  |  | 206.03 |  |  |
| Na | 879.57 | 301.69 | 947.45 | 126.40 | 554.49 | 28.59 | 403.18 |
| Fe | 596.57 | 3198.75 | 831.95 | 543.09 | 1278.06 | 140.49 | 9844.47 |
| Ni | 100.83 | 540.64 | 140.61 | 91.79 | 216.01 | 23.75 | 1663.85 |
| Cr | 142.84 | 765.90 | 199.20 | 130.03 | 306.02 | 33.64 | 2357.12 |

The motion of the control rod is shown in Figure 24.


Figure 24. The control rod "in" and "out" positions respect to driver and blanket subassemblies.

### 5.3 Input File Description

The DIF3D input file consists of my different cards describing the problem. In this simulation, only basic three cards, A.DIF3D, A.HMG4C and A.NIP3, were used. The input file can be written in either free format or according to the formats specified for each card type.

### 5.3.1 A.DIF3D Description

The A.DIF3D contains the calculational parameters, storage containers, and edit sentinels.


The card numbers represent the following:
The type 01 card is used for problem title.
The type 02 card is used for storage and dump specifications.

- 20000000 - pointer container array size in fast core memory (FCM) in real*8 words
- 100000000 - the pointer container array size in core memory (ECM) in real*8 words

The type 03 card is used for the problem control parameters.

- 1 - fixed source problem
- 2 - both real and adjoint solution
- 0 - Chebyshev acceleration of outer iterations is on
- 4500 - minimum plane-block size in real*8 words for I/O transfer in the the concurrent inner iteration strategy
- 500 - maximum number of outer iteration
- 0 - restart flag is off
- 1000000000 - job time limit
- 0 - performs the estimated number of inner iterations for each group
- 0 - no acceleration of optimum overrelaxation factor calculation
- 90 - number of optimum overrelaxation factor estimation iteration control

The type 04 card is used for editing options.

- 1 - print problem description edits
- 0 - no geometry map edits for region to mesh interval
- 0 - no geometry map edits for zone to mesh interval
- 00 - no edits for the scattering and principal cross sections and principal cross sections edits
- 000 - no edits for the group balance edits integrated over the reactor, region balance edits by group and region balance edits totals
- 00 - no edits for both region power and average power density edits and power density by mesh interval edits
- 000 - no edits for flux edit by region and group including group and region totals, total flux edit by mesh interval, and total flux edit by mesh interval and group
- 1 - print edits for the zone averaged real flux
- 1 - print edits for region averaged flux

The type 05 card is used for convergence criteria.

- $1.0 \mathrm{E}-5$ - the eigenvalue convergence criterion for steady state calculation
- $1.0 \mathrm{E}-5$ - the pointwise fission source convergence criterion for steady state shape calculation
- 1.0E-5 - the average fission source convergence criterion for steady state shape calculation

The type 06 card is used for other floating-point data.

- 1.0 - the $\mathrm{k}_{\text {eff }}$ of reactor
- 0.001 - any pointwise fission source will be neglected in pointwise fission source convergence test if it is less than this factor time fission source
- 0.04 - error reduction factor to be achieved by each series of inner iterations for each group during a shape calculation
- $14.30000+6$ - steady state reactor power (Watts)

The type 12 card is used for parameters for variational nodal option.

- $80801-8^{\text {th }}$ order source approximation, $8^{\text {th }}$ order flux approximation, and linear leakage approximation (DEFAULT)
- 33 - P3 flux expansion and P3 leakage expansion


### 5.3.2 A.NIP3 Description

The geometry description of DIF3D computer code is specified in A.NIP3. A small part of A.NIP3 used for EBR-II reactor geometry and the explanation of each card are shown below. The EBR-II input file is given in Appendix B.

```
DATASET=A.NIP3
01 33 GROUP FIXED-SOURCE TRANSPORT PROBLEM
02 0 050000 50000 0
03 120
04 2 2 2 2 2 2 2 2
09 Z 1 60.000
09 Z 1 120.000
09 Z 1 121.944
    Lower Blanket Fuel Region
14 DEPB NA23I 0.000761778
14 DEPB U235N 0.000044937U238N 0.014745338
14 DEPB FE__R 0.010127125NI__R 0.001628561CR__R 0.002604296
15 DEPBB FR1BB
15 DEPB FR1B
15 DEPBT FR1BT
15 FUELB FR1FB
15 FUEL FR1F
15 FUELT FR1FT
15 DEPTB FR1TB
15 DEPT FR1T
15 DEPTT FR1TT
19 SOURC1 1 33 662.517546E+07
29 5.80898 25 3
    DRIVER REGION
30 OREF 01 0.0 60.000
30 BOTS 01 60.000 120.000
30 BOT 01 120.000 172.070
30 FR1BB 01 172.070 178.737
30}\mathrm{ FR1B 01 178.737 224.457
30 FR1BT 01 224.457 232.553
30
30}\mathrm{ FR1F 01 234.458 270.577
30 FR1FT 01 270.577 278.527
30 FR1TB 01 278.527 281.689
30 FR1T 01 281.689 327.409
30 FR1TT 01 327.409 338.998
30 TOPS 01 338.998 388.998
30 OREF 01 388.998 550.000
```

The card numbers represent the following:
The type 01 card is used for problem title.
The type 02 card is used for input processing specifications.

- 0 - no debugging printout
- 0 - no geometry processing module edits
- 50000 - size of main core storage array for geometry processing module
- 50000 - size of main core storage array for cross-section processing module
- 0 - size of bulk core storage array for cross-section processing modules
- 0 - no pointer debugging edits for cross-section processing module
- 0 - no cross-section processing edits
- 0 - no region/mesh interval printer-plotter map editing
- 0 - no zone/mesh interval printer-plotter map editing

The type 03 card is used for problem geometry.

- 120 - geometry type: hexagonal-z, full core in plane

The type 04 card is used for external boundary conditions.

- 2 - boundary condition at lower " $x$ " boundary of reactor
- 2 - boundary condition at upper "x" boundary of reactor
- 2 - boundary condition at lower " $y$ " boundary of reactor
- 2 - boundary condition at upper " $y$ " boundary of reactor
- 2 - boundary condition at lower " $z$ " boundary of reactor
- 2 - boundary condition at upper " $z$ " boundary of reactor

The type 09 card is used for variable mesh structure.

- Z - coordinate direction
- 1 - number of interval
- 60.000 - upper coordinate

This card can be repeated for each interval.
The type 14 card is used for composition specification.

- DEPBB - composition label
- NA23I - material label
- 0.000761778 - atom density

This card can be repeated for all materials and compositions.
The type 15 card is used for region/composition correspondence.

- DEPB - composition label
- FR1B - region label defining region containing specified composition

The type 19 card is used for region or mesh distributed inhomogeneous source.

- SOURC1 - label or region where source is located
- 1 - higher-energy group number
- 33 - lower-energy group number
- $662.517546 \mathrm{E}+07$ - isotopic source value in the specified mesh interval (neutrons per second per unit volume)

The type 29 card is used for hexagon dimension.

- 5.80898 - dimension of hexagon across flats
- 25 - total number of hexagonal rings
- 3-54 mesh points

The type 30 card is used for region definitions for arrays of hexagons.

- OREF - region label
- 01 - hexagonal ring number where region is located
- 0.0 - starting hexagon position for this region
- 60.000 - final hexagon position for this region

This card can be repeated for entire problem geometry.

### 5.3.3 A.HMG4C Description

HMG4C is designed to create a homogenized macroscopic cross-section for each composition.

| UNFORM=A.HMG4C |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 01 | TURN OFF HMG4C EDITS |  |  |  |  |  |  |
| 02 | 999999 | 1 | 0 | 0 | 0 |  | 1 |

The card numbers represent the following:

The type 01 card is used for problem title.
The type 02 card is used for problem options

- 999999 - size of main core container array
- 1 - suppress all printing except diagnostics
- 0 - no COMPXS edit
- 0 - no ISOTXS edit
- 0 - no POINTR debugging edit
- 1 - use isotope fission vectors to compute composition fission vectors with total fission source weighting


### 5.4 Running DIF3D

The DIF3D model of the EBR-II reactor was run on Idaho National Laboratory's (INL) High Performance Computing (HPC) cluster. DIF3D calculated the flux and adjoint flux for the fixed-source problem. The run time for the simulation ranged between 3 hours to 8 hours depending on the amount of fuel in the reactor. The run time on a regular home computer with 32GB RAM was ranging between 8 hours to 2 days depending on the amount of fuel material. The process of installing DIF3D on the HPC required experience working in Linux environment. The detailed protocol is given in Appendix A.

### 5.5 Dry and Wet Critical Simulation Failures

The approach-to-critical simulation of EBR-II using the DIF3D computer code started with all control rods and safety rods inserted, and every outer blanket assembly inserted. The neutron flux was calculated in all detector positions. Figure 25 to Figure 28 show the $1 / \mathrm{M}$ of detectors 1 to 4 as a function of number of assemblies, respectively. As fuel was added to the reactor, the neutron flux increases and inverse flux decreases. First six data points of the plot show that as the number of fuel assemblies was increased, the inverse flux was decreased. But starting seventh data point, the inverse flux increased. After carefully reviewing the input file and atom density calculation, it was found that the ${ }^{235} \mathrm{U}$ and ${ }^{238} \mathrm{U}$ atom density calculation of blanket assemblies was missing division of 100 in the percentage calculation.


Figure 25. Dry critical experiment initial flux calculation in detector \#1.


Figure 26. Dry critical experiment initial flux calculation in detector \#2.


Figure 27. Dry critical experiment initial flux calculation in detector \#3.


Figure 28. Dry critical experiment initial flux calculation in detector \#4.

After fixing the error, both dry and wet critical experiment were simulated again. The wet critical experiment's detector responses are shown in Figure 29. The inverse flux value decreases as the number of fuel assemblies increases as expected. The dry critical experiment results improved compared to the previous simulation, however, the Figure 30 shows that the inverse flux value did not decrease after approaching 60 assemblies.


Figure 29. Wet critical experiment, CR* "in" position, 1/flux plot.
CR - Control Rods


Figure 30. Dry critical experiment, CR "in" position, 1/flux plot.

However, the dry critical simulation result did not show as much increase in the inverse flux value, it was still not decreasing consistently as fuel being added. Both dry and wet critical experiment literature was reviewed again to help identify possible mistakes. From Figure 30, we can see that driver region fuel loading was going as predicted. However, when it came to adding the inner blanket region, the flux started decreasing. These calculations assumed enrichment of the inner blanket was $0.3 \%{ }^{235} \mathrm{U}$. However, the dry and wet critical experiment documents said that when they operated EBR-II during both dry and wet critical experiment, there was an assembly called "enriched inner blanket". The enrichment of the enriched inner blanket assemblies was assumed to be the same as driver assembly enrichment, $48.08 \mathrm{wt} \%{ }^{235} \mathrm{U}$. With the enrichment of inner blanket assembly increased to $48.08 \mathrm{wt} \%{ }^{235} \mathrm{U}$, the simulation was ended with the result which is shown in Figure 31. The dimensions of the fuel slug remained same as inner blanket fuel slug.


Figure 31. Dry critical experiment, CR "in" position, 1/flux plot with enriched inner blanket.

As Figure 31 shows, the data points are in a decreasing order, which we were not able to see before. But, the amount of ${ }^{235} \mathrm{U}$ was too large. A single enriched inner blanket assembly contained 22.6 kg of ${ }^{235} \mathrm{U}$. From Table 5 and Table 6, the amount of ${ }^{235} \mathrm{U}$ is calculated to be 2.83 kg per inner blanket assembly. Because of it is greater length and 19 large pins, the $48.08 \%$ enriched inner blanket assembly had nearly 10 times more ${ }^{235} \mathrm{U}$ than the driver assembly. It was assumed that the "enriched inner blanket" assemblies were a regular driver assembly. Hence, instead of putting enriched inner blanket in the model, a regular driver assembly was used for comparison purposes. The revised dry and wet critical experiment results are shown in Figure 32 and Figure 33, respectively.


Figure 32. Dry critical experiment, CR "in" position, driver fuel subassemblies added as an inner blanket.


Figure 33. Wet critical experiment, CR "in" position, driver fuel subassemblies added as an inner blanket.

The dry critical experiment data points were clearly in descending order. However, the wet critical experiment data points look like descending order as shown in Figure 33, the last three points are not clear. So, these last three points were plotted on a separate scale to verify the $1 / \mathrm{M}$ curve. The last three data points of detector 1 and 2 were plotted as shown in Figure 34 and Figure 35, respectively.


Figure 34. Wet critical experiment, CR "in", the last three points of detector 1.


Figure 35. Wet critical experiment, CR "in", the last three points of detector 2.

In the second from the last fuel loading stage, the inverse flux value increased. Substituting enriched inner blanket assemblies by regular driver assembly did not work in wet critical experiment simulation. Further investigation was needed.

As mentioned in the literature, the inner blanket subassembly with enriched fuel was used for further parametric study. Both dry and wet critical experiments were repeated with an enriched inner blanket subassembly. The difference between the previous enriched inner blanket assembly is that the enrichment is not $48.0 \mathrm{wt} \%{ }^{235} \mathrm{U}$. The enriched inner blanket assembly now had the same amount of ${ }^{235} \mathrm{U}$, which is 2.82 kg of ${ }^{235} \mathrm{U}$ per assembly. The rest of the fuel consisted of pure ${ }^{238} \mathrm{U}$. The total amount of uranium in each inner blanket and outer blanket assemblies was calculated to be 47.1 kg . The dry critical experiment simulation results are plotted as shown in Figure 36.


Figure 36. Dry critical experiment, CR "in" position, with enriched inner blanket.

The shape of the simulated detector response was very similar to the measured results. The detector 2 was chosen randomly to verify the $1 / \mathrm{M}$ shape. The $1 / \mathrm{M}$ plot of simulated detector 2 response and measured detector 2 results are shown in Figure 37 and Figure 38, respectively.


Figure 37. Simulated detector 2 response.


Figure 38. Measured detector 2 response.
Since the Y-axis values are not the same, the data normalized for comparison. The normalized detector 2 response is plotted in Figure 39.


Figure 39. The normalized detector 2 responses.
Since the dry critical simulation results looked more like a curve (Figure 36) than a straight line (Figure 32), the wet critical experiment was simulated with same enriched inner blanket subassemblies. The 1/M curve of the wet critical experiment with control rod "in" position is shown in Figure 40. The detectors 1 and 2 were randomly chosen to verify whether there was a flaw in the flux behavior as before. The detector 1 and 4 results are shown in Figure 41 and Figure 42, respectively.


Figure 40. Wet critical experiment, CR "in" position, with enriched inner blanket.


Figure 41. Wet critical experiment, CR "in" position, the detector 1 response.


Figure 42. Wet critical experiment, CR "in" position, the detector 4 response.

To confirm continuous decrease in the inverse flux value, the last four points of detector 1 and 4 were plotted separately in Figure 43 and Figure 44, respectively.


Figure 43. Wet critical experiment, CR "in", the last three points of detector 1.


Figure 44. Wet critical experiment, CR "in", the last three points of detector 4.

Now that every data point in the dry and wet critical experiment were in descending orders and the shape looks more curve like, the enriched inner blanket assembly with $2.82 \mathrm{~kg}{ }^{235} \mathrm{U}$ was used during approach-to-critical experiment simulation. With these results, the simulation of dry and wet critical approach-to-critical experiments were successful.

## 6. MSM Correction Factor

After simulating the approach-to-critical experiments, the measured results of the same experiment can be corrected by MSM correction factor as discussed in Section 2.

### 6.1 Calculating MSM Correction Factor

The MSM correction factor is calculated by Equation 11 (page 16) in each fuel loading stage. Every variable in this equation is calculated by DIF3D. Let's take the fuel loading stage 1 (Figure 13) and 2 (Figure 14) of dry critical control rods up position for example. The three parts, $\left\langle\phi^{*} S\right\rangle,\left\langle\phi^{*} \mathrm{~F} \phi\right\rangle$, and $\left\langle\Sigma_{d} \phi\right\rangle$, of the Equation 11 will be evaluated separately in each stage.

$$
\begin{aligned}
& \left\langle\phi^{*} S\right\rangle=\int_{E} \phi^{*}(E) S d V=\sum_{n=1}^{33} \phi^{*}\left(E_{n}\right) S V \\
& \left\langle\phi^{*} \mathrm{~F} \phi\right\rangle=\int_{E} \phi^{*}(E) v \Sigma_{f}(E) \phi(E) d V=\sum_{n=1}^{33} \phi^{*}\left(E_{n}\right) v \Sigma_{f}\left(E_{n}\right) \phi\left(E_{n}\right) V \\
& \left\langle\Sigma_{d} \phi\right\rangle=\int_{E} \Sigma_{d}(E) \phi(E) d V=\sum_{n=1}^{33} \Sigma_{d}\left(E_{n}\right) \phi\left(E_{n}\right) V
\end{aligned}
$$

The calculated values are given in Table 11.
Table 11. The Calculated Values of Each Variable*

|  | $\left\langle\phi^{*} S\right\rangle$ | $\left\langle\phi^{*} \mathrm{~F} \phi\right\rangle$ | $\left\langle\Sigma_{d} \phi\right\rangle_{1}$ | $\left\langle\Sigma_{d} \phi\right\rangle_{2}$ | $\left\langle\Sigma_{d} \phi\right\rangle_{3}$ | $\left\langle\Sigma_{d} \phi\right\rangle_{4}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Stage 1 | $9.75 \mathrm{E}+14$ | $8.04 \mathrm{E}+20$ | $3.64 \mathrm{E}+08$ | $4.97 \mathrm{E}+08$ | $7.68 \mathrm{E}+08$ | $7.70 \mathrm{E}+08$ |
| Stage 2 | $9.87 \mathrm{E}+14$ | $1.86 \mathrm{E}+21$ | $4.69 \mathrm{E}+08$ | $6.23 \mathrm{E}+08$ | $9.46 \mathrm{E}+08$ | $9.31 \mathrm{E}+08$ |

*Flux is arbitrary from the DIF3D calculation
The calculated correction factors for each detector are shown in Table 12.

Table 12. MSM Correction Factor for Each Detector

|  | Detector 1 | Detector 2 | Detector 3 | Detector 4 |
| :--- | :---: | :---: | :---: | :---: |
| Stage 1 | 0.56576 | 0.54928 | 0.54019 | 0.52977 |
| Stage 2 | 0.40486 | 0.36229 | 0.35256 | 0.35254 |

The $1 / \mathrm{M}$ value of the measured data is corrected by multiplying it by the ratio of MSM correction factors. Both measured and corrected $1 / \mathrm{M}$ values are shown in Table 13.

Table 13. Detector Response before and after MSM Correction

|  | Detector 1 | Detector 2 | Detector 3 | Detector 4 |
| :--- | :---: | :---: | :---: | :---: |
| Measured 1/M | 0.22389 | 0.60125 | 0.48245 | 0.44528 |
| Corrected 1/M | 0.12667 | 0.33026 | 0.26062 | 0.23590 |

The range of the corrected $1 / \mathrm{M}$ values is 0.20359 and the range of uncorrected $1 / \mathrm{M}$ value is 0.37736 . The data points got closer which is the purpose of MSM. The MSM correction factors were calculated for each detector at each stage of the approach-to-critical experiments.

### 6.2 Applying MSM Correction on ASM results

The measured detector response of EBR-II reactor dry and wet critical experiment data was corrected using MSM correction factors. Table 14 and Table 15 show the measured $1 / \mathrm{M}$ value, MSM correction factor, and corrected $1 / \mathrm{M}$ value of dry and wet critical experiments with control rods "in" position, respectively. Table 16 and Table 17 show the measured $1 / \mathrm{M}$ value, MSM correction factor, and corrected $1 / \mathrm{M}$ value of dry and wet critical experiments with control rods "out/down" position, respectively.

Table 14. Dry Critical Experiment, CR "in", MSM Correction

| \# of fuel assemblies | Measured 1/M Value |  |  |  | Correction Factors |  |  |  | MSM Corrected 1/M Value |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Det 1 | Det 2 | Det 3 | Det 4 | Det 1 | Det 2 | Det 3 | Det 4 | Det 1 | Det 2 | Det 3 | Det 4 |
| 31 | 0.2239 | 0.6012 | 0.4825 | 0.4453 | 0.5658 | 0.5493 | 0.5402 | 0.5298 | 0.1267 | 0.3303 | 0.2606 | 0.2359 |
| 40 | 0.1502 | 0.4000 | 0.3022 | 0.2785 | 0.4049 | 0.3623 | 0.3526 | 0.3525 | 0.0608 | 0.1449 | 0.1065 | 0.0982 |
| 49 | 0.0878 | 0.2299 | 0.1678 | 0.1513 | 0.2870 | 0.2375 | 0.2255 | 0.2325 | 0.0252 | 0.0546 | 0.0378 | 0.0352 |
| 55 | 0.0565 | 0.1468 | 0.1048 | 0.0938 | 0.2463 | 0.1964 | 0.1843 | 0.1930 | 0.0139 | 0.0288 | 0.0193 | 0.0181 |
| 61 | 0.0345 | 0.0898 | 0.0630 | 0.0561 | 0.1941 | 0.1497 | 0.1389 | 0.1476 | 0.0067 | 0.0134 | 0.0088 | 0.0083 |
| 67 | 0.0217 | 0.0552 | 0.0374 | 0.0330 | 0.1714 | 0.1310 | 0.1213 | 0.1294 | 0.0037 | 0.0072 | 0.0045 | 0.0043 |
| 73 | 0.0102 | 0.0257 | 0.0172 | 0.0146 | 0.1539 | 0.1171 | 0.0907 | 0.1157 | 0.0016 | 0.0030 | 0.0016 | 0.0017 |
| 77 | 0.0065 | 0.0162 | 0.0106 | 0.0089 | 0.1409 | 0.1058 | 0.0976 | 0.1049 | 0.0009 | 0.0017 | 0.0010 | 0.0009 |
| 83 | 0.0018 | 0.0043 | 0.0028 | 0.0023 | 0.1216 | 0.0914 | 0.0839 | 0.0906 | 0.0002 | 0.0004 | 0.0002 | 0.0002 |

Table 15. Wet Critical Experiment, CR "in", MSM Correction

| \# of fuel assemblies | Measured 1/M Value |  |  |  |  | Correction Factors |  |  |  |  | MSM Corrected 1/M Value |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Det 1 | Det 2 | Det 3 | Det 4 | Det 5 | Det 1 | Det 2 | Det 3 | Det 4 | Det 5 | Det 1 | Det 2 | Det 3 | Det 4 | Det 5 |
| 31 | 0.3857 | 0.3778 | 0.3742 | 0.4361 | 0.4898 | 1.1410 | 1.1410 | 1.0015 | 1.0273 | 0.9971 | 0.4401 | 0.4310 | 0.3747 | 0.4480 | 0.4883 |
| 37 | 0.2590 | 0.2629 | 0.2568 | 0.3166 | 0.3651 | 1.2369 | 1.2369 | 0.9747 | 1.0015 | 1.0537 | 0.3203 | 0.3252 | 0.2503 | 0.3171 | 0.3847 |
| 43 | 0.1695 | 0.1678 | 0.1689 | 0.2170 | 0.2664 | 1.0432 | 1.0432 | 0.8283 | 0.8460 | 0.8027 | 0.1769 | 0.1750 | 0.1399 | 0.1835 | 0.2138 |
| 49 | 0.0936 | 0.0940 | 0.0943 | 0.1264 | 0.1629 | 0.6444 | 0.6444 | 0.5171 | 0.5268 | 0.4539 | 0.0603 | 0.0606 | 0.0488 | 0.0666 | 0.0740 |
| 55 | 0.0478 | 0.0472 | 0.0472 | 0.0721 | 0.0896 | 0.7029 | 0.7029 | 0.5668 | 0.5767 | 0.4712 | 0.0336 | 0.0332 | 0.0267 | 0.0416 | 0.0422 |
| 60 | 0.0229 | 0.0226 | 0.0227 | 0.0389 | 0.0480 | 0.4738 | 0.4738 | 0.3842 | 0.3907 | 0.3044 | 0.0108 | 0.0107 | 0.0087 | 0.0152 | 0.0146 |
| 64 | 0.0102 | 0.0097 | 0.0100 | 0.0141 | 0.0252 | 0.4056 | 0.4056 | 0.3324 | 0.3379 | 0.2551 | 0.0041 | 0.0039 | 0.0033 | 0.0048 | 0.0064 |
| 67 | 0.0022 | 0.0036 | 0.0037 | 0.0052 | 0.0150 | 0.5532 | 0.5532 | 0.4749 | 0.4831 | 0.3581 | 0.0012 | 0.0020 | 0.0018 | 0.0025 | 0.0054 |

Table 16. Dry Critical Experiment, CR "out", MSM Correction

| \# of fuel <br> assemblies | Measured 1/M Value |  |  |  | Correction Factors |  |  |  | MSM Corrected 1/M Value |  |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Det 1 | Det 2 | Det 3 | Det 4 | Det 1 | Det 2 | Det 3 | Det 4 | Det 1 | Det 2 | Det 3 | Det 4 |
| 31 | 0.2380 | 0.6223 | 0.4088 | 0.3605 | 0.4423 | 0.4416 | 0.4360 | 0.4447 | 0.1053 | 0.2748 | 0.1782 | 0.1603 |
| 40 | 0.1665 | 0.4283 | 0.2553 | 0.2232 | 0.3067 | 0.2864 | 0.2808 | 0.2908 | 0.0511 | 0.1227 | 0.0717 | 0.0649 |
| 49 | 0.1048 | 0.2624 | 0.1489 | 0.1267 | 0.2318 | 0.2031 | 0.1951 | 0.2072 | 0.0243 | 0.0533 | 0.0291 | 0.0263 |
| 55 | 0.0723 | 0.1795 | 0.0994 | 0.0860 | 0.2132 | 0.1807 | 0.1715 | 0.1851 | 0.0154 | 0.0324 | 0.0171 | 0.0159 |
| 61 | 0.0500 | 0.1233 | 0.0676 | 0.0571 | 0.1863 | 0.1533 | 0.1441 | 0.1575 | 0.0093 | 0.0189 | 0.0097 | 0.0090 |
| 67 | 0.0349 | 0.0844 | 0.0447 | 0.0373 | 0.1287 | 0.1048 | 0.0983 | 0.1079 | 0.0045 | 0.0088 | 0.0044 | 0.0040 |
| 73 | 0.0200 | 0.0477 | 0.0250 | 0.0202 | 0.1471 | 0.1190 | 0.1109 | 0.1227 | 0.0029 | 0.0057 | 0.0028 | 0.0025 |
| 77 | 0.0157 | 0.0371 | 0.0191 | 0.0152 | 0.1384 | 0.1106 | 0.1034 | 0.1144 | 0.0022 | 0.0041 | 0.0020 | 0.0017 |
| 83 | 0.0107 | 0.0240 | 0.0126 | 0.0100 | 0.1249 | 0.0999 | 0.0930 | 0.1033 | 0.0013 | 0.0024 | 0.0012 | 0.0010 |
| 87 | 0.0079 |  | 0.0091 | 0.0073 | 0.1192 | 0.0945 | 0.0883 | 0.0980 | 0.0009 |  | 0.0008 | 0.0007 |

Table 17. Wet Critical Experiment, CR "out", MSM Correction

| \# of fuel assemblies | Measured 1/M Value |  |  |  |  | Correction Factors |  |  |  |  | MSM Corrected 1/M Value |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Det 1 | Det 2 | Det 3 | Det 4 | Det 5 | Det 1 | Det 2 | Det 3 | Det 4 | Det 5 | Det 1 | Det 2 | Det 3 | Det 4 | Det 5 |
| 31 | 0.2700 | 0.2615 | 0.2582 | 0.2731 | 0.2981 | 0.6722 | 0.6722 | 0.6899 | 0.6811 | 0.5822 | 0.1815 | 0.1758 | 0.1782 | 0.1861 | 0.1736 |
| 37 | 0.1843 | 0.1882 | 0.1797 | 0.1927 | 0.2153 | 0.5391 | 0.5391 | 0.5629 | 0.5530 | 0.4571 | 0.0993 | 0.1014 | 0.1012 | 0.1065 | 0.0984 |
| 43 | 0.1292 | 0.1275 | 0.1230 | 0.1379 | 0.1629 | 0.4236 | 0.4236 | 0.4462 | 0.4356 | 0.3284 | 0.0547 | 0.0540 | 0.0549 | 0.0601 | 0.0535 |
| 49 | 0.0771 | 0.0775 | 0.0743 | 0.0873 | 0.1049 | 0.3615 | 0.3615 | 0.3847 | 0.3746 | 0.2574 | 0.0279 | 0.0280 | 0.0286 | 0.0327 | 0.0270 |
| 55 | 0.0450 | 0.0440 | 0.0436 | 0.0551 | 0.0645 | 0.3224 | 0.3224 | 0.3448 | 0.3353 | 0.2197 | 0.0145 | 0.0142 | 0.0150 | 0.0185 | 0.0142 |
| 60 | 0.0290 | 0.0283 | 0.0279 | 0.0404 | 0.0443 | 0.2715 | 0.2715 | 0.2919 | 0.2837 | 0.1786 | 0.0079 | 0.0077 | 0.0082 | 0.0115 | 0.0079 |
| 64 | 0.0195 | 0.0186 | 0.0185 |  | 0.0311 | 0.2418 | 0.2418 | 0.2626 | 0.2551 | 0.1555 | 0.0047 | 0.0045 | 0.0049 |  | 0.0048 |
| 67 | 0.0140 | 0.0138 | 0.0139 | 0.0172 | 0.0243 | 0.2236 | 0.2236 | 0.2547 | 0.2475 | 0.1466 | 0.0031 | 0.0031 | 0.0035 | 0.0042 | 0.0036 |
| 70 | 0.0105 | 0.0103 | 0.0104 | 0.0138 | 0.0176 | 0.2108 | 0.2108 | 0.2400 | 0.2333 | 0.1395 | 0.0022 | 0.0022 | 0.0025 | 0.0032 | 0.0025 |

The measured detector response and corresponding MSM correction of the dry critical experiment with control rod "in" position are shown in Figure 45 and Figure 46, respectively. However, while the data points got closer, it was difficult to see it. The last six data points are plotted separately on Figure 47 and Figure 48. The last four data points are plotted separately on Figure 50 and Figure 51.


Figure 45. Dry critical experiment, CR "in" position, measured detector response.


Figure 46. Dry critical experiment, CR "in" position, the detector response after MSM correction.


Figure 47. Dry critical experiment, CR "in", last six measured data points.


Figure 48. Dry critical experiment, CR "in", last six MSM corrected data points.

As shown in Figure 49, the corrected 1/M plot of the last six points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 49. Dry critical experiment, CR "in", amplified the last six MSM corrected data points.


Figure 50. Dry critical experiment, CR "in", last four measured data points.


Figure 51. Dry critical experiment, CR "in", last four MSM corrected data points.

As shown in Figure 52, the corrected 1/M plot of the last four points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 52. Dry critical experiment, CR "in", amplified the last four MSM corrected data points.

The measured detector response and corresponding MSM correction of the dry critical experiment with control rod "out" position are shown in Figure 53 and Figure 54, respectively. However, while the data points got closer, it was difficult to see it. The last seven data points are plotted separately on Figure 55 and Figure 56. The last four data points are plotted separately on Figure 58 and Figure 59.


Figure 53. Dry critical experiment, CR "out" position, measured detector response.


Figure 54. Dry critical experiment, CR "out" position, the detector response after MSM correction.


Figure 55. Dry critical experiment, CR "out", last seven measured data points.


Figure 56. Dry critical experiment, CR "out", last seven MSM corrected data points.

As shown in Figure 57, the corrected 1/M plot of the last seven points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 57. Dry critical experiment, CR "out", amplified the last seven MSM corrected data points.


Figure 58. Dry critical experiment, CR "out", last four measured data points.


Figure 59. Dry critical experiment, CR "out", last four MSM corrected data points.

As shown in Figure 60, the corrected 1/M plot of the last four points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 60. Dry critical experiment, CR "out", amplified the last four MSM corrected data points.

The measured detector response and corresponding MSM correction of the wet critical experiment with control rod "in" position are shown in Figure 61 and Figure 62, respectively. However, while the data points got closer, it was difficult to see it. The last five data points are plotted separately on Figure 63 and Figure 64. The last three data points are plotted separately on Figure 66 and Figure 67.


Figure 61. Wet critical experiment, CR "in" position, measured detector response.


Figure 62.Wet critical experiment, CR "in" position, the detector response after MSM correction.


Figure 63. Wet critical experiment, CR "in", last five measured data points.


Figure 64. Wet critical experiment, CR "in", last five MSM corrected data points.

As shown in Figure 65, the corrected 1/M plot of the last five points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 65. Wet critical experiment, CR "in", amplified the last five MSM corrected data points.


Figure 66. Wet critical experiment, CR "in", last three measured data points.


Figure 67. Wet critical experiment, CR "in", last five MSM corrected data points.

As shown in Figure 68, the corrected $1 / \mathrm{M}$ plot of the last three points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 68. Wet critical experiment, CR "in", amplified the last five MSM corrected data points.

The measured detector response and corresponding MSM correction of the wet critical experiment with control rod "out" position are shown in Figure 69 and Figure 70, respectively. However, while the data points got closer, it was difficult to see it. The last six data points are plotted separately on Figure 71 and Figure 72. The last three data points are plotted separately on Figure 74 and Figure 75.


Figure 69. Wet critical experiment, CR "out" position, measured detector response.


Figure 70. Wet critical experiment, CR "out" position, the detector response after MSM correction.


Figure 71. Wet critical experiment, CR "out", last six measured data points.


Figure 72. Wet critical experiment, CR "out", last six MSM corrected data points.

As shown in Figure 73, the corrected 1/M plot of the last six points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 73. Wet critical experiment, CR "out", amplified the last six MSM corrected data points.


Figure 74. Wet critical experiment, CR "out", last three measured data points.


Figure 75. Wet critical experiment, CR "out", last three MSM corrected data points.

As shown in Figure 76, the corrected 1/M plot of the last six points is amplified to show better detector $1 / \mathrm{M}$ locations.


Figure 76. Wet critical experiment, CR "out", amplified the last three MSM corrected data points.

### 6.3 The Improvement Factor

The improvement factor (IF) is a quantity that represents the quality of the application of MSM correction. The IF is calculated from the data point range. According to $1 / \mathrm{M}$, extrapolation of any two consecutive points will give the predicted number of fuel assemblies required for a reactor to go critical. Since there is more than one detector in the system, we get more than one prediction for criticality. The range of this criticality prediction is important. For example, Figure 77 shows that two detectors each have different $1 / \mathrm{M}$ values predicting criticality at two different points.


Figure 77. Two detectors response at two different stages before MSM correction.

The orange detector predicts 60 fuel assemblies to go critical and blue detector predicts 62.5 fuel assemblies to go critical. The range is 2.5 . In the EBR-II case, we have more than two detectors. In which case, we take the difference between the maximum and minimum predicted values. Although, this range is important, the $1 / \mathrm{M}$ range also important. The IF is a ratio of MSM and ASM factors. The MSM and ASM factors are multiplication of three
numbers; range in criticality prediction, range in first reactor configuration and range in second reactor configuration. he improvement factor is shown in Equation 17.

$$
\begin{gather*}
I F=\frac{\text { MSM Factor }}{\text { ASM Factor }}  \tag{47}\\
\text { ASM Factor }=A * B * C \tag{58}
\end{gather*}
$$

Where:

A - Maximum distance between first data points on ASM plot
B - Maximum distance between second data points on ASM plot
C - Maximum distance between predicted criticality on ASM plot

$$
\begin{equation*}
\text { MSM Factor }=A^{\prime} * B^{\prime} * C^{\prime} \tag{69}
\end{equation*}
$$

Where:

A' - Maximum distance between first data points on MSM plot
B' - Maximum distance between second data points on MSM plot C' - Maximum distance between predicted criticality on MSM plot

From the example that was used for the range of the criticality prediction, the range in first and second configuration can be calculated. It is the difference between the minimum and maximum points in each configuration. Thus, the range in the first configuration is 0.2 and the range in second configuration is 0.15 . Hence, the ASM factor is equal to 0.075 . The optimal quantity is zero for both ASM and MSM factors.

Now assume we had MSM correction on the previous ASM example. Figure 78 shows the corrected $1 / \mathrm{M}$ values for each detector at each stage. The range in criticality prediction is 1.25 . The range got shorter by applying MSM correction, but it does not
always work in our favor. Sometimes the range gets bigger. That is why this range cannot quantify the quality of MSM correction alone.


Figure 78. Two detectors response at two different stages after MSM correction.

The range in first and second configurations became 0.07 and 0.06 , respectively. Hence, the MSM factor is equal to 0.00525 and the IF is 0.07 . If the IF was equal to 1 , there was no improvement. If the IF is less than 1 , the MSM correction was applied successfully. However, the smaller the IF, better the correction. In theory, the best value for IF is 0 . If the IF is greater than 1, the MSM correction to the existing ASM is failed.

The Table 18 shows the IF of the EBR-II dry and wet critical experiments. As the values indicate, overall MSM correction was applied very well. The first two points of the wet critical experiment with control rod "in" position, was not corrected well.

Table 18. The Improvement Factor

|  | Dry Crit. <br> Rods "out" | Dry Crit. <br> Rods "in" | Wet Crit. <br> Rods "out" | Wet Crit. <br> Rods "in" |
| :--- | :---: | :---: | :---: | :---: |
| Loading 3 and 4 | 0.046 | 0.114 | 0.025 | 1.199 |
| Loading 4 and 5 | 0.030 | 0.050 | 0.006 | 1.155 |
| Loading 5 and 6 | 0.043 | 0.038 | 0.016 | 0.206 |
| Loading 6 and 7 | 0.018 | 0.022 | 0.026 | 0.049 |
| Loading 7 and 8 | 0.004 | 0.009 | 0.021 | 0.031 |
| Loading 8 and 9 | 0.021 | 0.021 | 0.002 | 0.012 |
| Loading 9 and 10 | 0.010 | 0.031 | 0.003 | 0.013 |
| Loading 10 and 11 | 0.007 | 0.005 | 0.007 |  |
| Loading 11 and 12 | 0.011 |  |  |  |

## 7. Summary and Conclusion

Every nuclear reactor starts with a subcritical configuration and slowly approaches criticality. Traditionally, the ASM method was used to predict criticality. However, this method has a weakness. The more precise method, called MSM, was developed to improve ASM. This research was focused on applying MSM correction on measured ASM results of the dry and wet critical experiments of EBR-II reactor. There are four sets of measured data of EBR-II experiments: dry critical experiment with all control rods inserted and removed, wet critical experiment with all control rods inserted and removed.

The MSM corrections of dry critical experiments (both control rods inserted and removed positions) were successful. The data points of $1 / \mathrm{M}$ curve get closer to each other and the improvement factor is below 1 .

The MSM corrections of wet critical experiments were successful except the first two data points of control rods inserted configuration. When starting the wet critical experiment, the $\mathrm{k}_{\text {eff }}$ was close to zero and count rate was about 100 counts per minute. The difference between dry and wet critical experiments is that the neutron detectors were located in different positions. The neutron detectors in dry critical experiments were in the reactor core specifically in inner blanket and outer blanket subassemblies. The neutron detectors in the wet critical experiment were located in the J-thimbles outside of the core. The DIF3D was not able to model the detectors outside of the core. Thus, the detector locations in the wet critical experiments were in the very outer row of the outer blanket region. They were located such that the reactor core, DIF3D detector, and actual detector in a line and the DIF3D detector was as close as possible to the actual detector.

As seen on measured $1 / \mathrm{M}$ plots, every detector predicts different criticality. The MSM method corrects these detector responses and predicts better criticality. To apply this technique on a reactor startup, the DIF3D simulation must be done beforehand because every simulation took between 3 to 6 hours on INL HPC. Doing simulation after taking every count rate is impractical. Hence, the simulation of approach-to-critical and calculation of MSM correction factor should be done before reactor startup. With calculated MSM correction factors in each fuel loading stage, the count rates can be corrected right after it is taken and predict better criticality.

## 8. References

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## Appendix A

## Setting up INL HPC Account and Installing DIF3D

After setting a PIN, install ssh on Linux machine by: sudo apt-get install ssh

Search a folder named "ssh". Open "ssh_config". In the very end of the file, add the following:

Host hpclogin hpclogin.inl.gov

User YourHpcUsername
HostName hpclogin.inl.gov
LocalForward 8080 hpcweb:88
Then save and close.
Now open Terminal and login to hpc by typing:
ssh YourUserName@hpclogin.inl.gov
enter your password which is your 8-DIGIT-PIN+6 digit token.

To copy a file from your computer, use SCP.
Open a new terminal and type following to copy a file:
scp fileLocation YourUserName@hpclogin.inl.gov:
enter the password.
The file will be copied to your home directory in hpc. You can move the file by "mv" command when you log in to hpc.

To get MCNP permission, go to the Request History link on RSICC's Customer Service homepage. Click on the "Request History" link and enter your RSICC Pass number and Password. Once you verify the information is correct, an email will be sent to the email
address listed in your account. Forward this email to rsicc_licenses@inl.gov. You will receive an email from INL that you have a permission to use MCNP or other RSICC codes on HPC.

To use MCNP
First you need to $\log$ in to the server, falcon1, falcon2, bechler etc.
ssh falcon1
Inside falcon1, your directories are same as hpclogin.
Do the following commands based on your MCNP version.
module load use.exp_ctl
module load MCNP6/1.0-imvmklt-1.5.0

To see available options of MCNP type:
sub_menp6_1.0-h
sub_menp6_1.0 -i inputfilenameOrLocation -w walltime -P projectname -x locationORnameOfthecrossection -n numberofbatch -N numberofcpu -j jobname For example:
sub_menp6_1.0 -i EBRII.i -w 24:0:0 -P neup -x EBRII646dir -n 240 -N 24 -j EBR2 For DIF3D, you need to compile it on HPC.

First you will need to copy the DIF3D.tar.gz file to your HPC directory. scp locationOfyourDIF3D.tar.gz YourUserName@ hpclogin.inl.gov:
log in to your hpc account then extract the DIF3D.tar.gz file.
tar -xvzf DIF3D.tar.gz
After it is extracted, go into extracted folder and rename "Makefile.arch.export" to "Makefile.arch"
rm "Makefile.arch.export" "Makefile.arch"
then open the file
vi Makefile.arch
hit "i"
replace everything by:
$\mathrm{FC}=$ gfortran
$\mathrm{CC}=\mathrm{gcc}$
LD $=$ gfortran
CPPDEF = -DVERSION_STANDALONE -DFORCEFIXED -DISABLE_TIMING
FFLAGS = -02 -DMEMORY_LARGE -fpic
CFLAGS =
Hit "esc" and hit "." then type "wq" and hit enter.
Now go to the folder named "src_DIF3D"
And type "make -j4"
It will compile dif3d on your hpc.
Copy the executable of dif3d which is named by "dif3d.x" to the location you want cp -i dif3d.x locationYouWant

In order to run dif3d, you will need cross section file, input file and dif3d.x in a same location.

After you have all 3 of them in a same location, you will need a shell script to run dif3d on hpc. Create a text file and name it MyFile.sh

This file must contain the following:
\#!/bin/bash
\#PBS -N nameofyourwork
\#PBS - ј oe
\#PBS -P neup
\#PBS -1 select $=1:$ ncpus $=1:$ mem $=100 \mathrm{gb}$
cd locationOfyourworkingfolder
./dif3d.x <inputfile.inp >outputfile
Copy this MyFile.sh from your computer to the hpc and then copy it to the directory where your dif3d.x and input files are.

Then log in to hpc and the log in to bechler bechler server by:
ssh bechler
now go into the directory where MyFile.sh is.
Type
qsub -1 walltime=24:0:0 MyFile.sh
If you know that your work will take more than 24 hours, then increase it.
After submitting a job, you will receive a job ID number. You can check the status of your work by:
qstat jobIDnumber

## Appendix B

Input deck of dry critical experiment with control rods "in" position, the last fuel loading configuration.


| 09 | $Z$ | 1 | 270.577 |
| :--- | :--- | :--- | :--- |
| 09 | $Z$ | 1 | 277.892 |
| 09 | $Z$ | 1 | 278.527 |
| 09 | $Z$ | 1 | 281.689 |
| 09 | $Z$ | 1 | 282.337 |
| 09 | $Z$ | 1 | 287.722 |
| 09 | $Z$ | 1 | 297.897 |
| 09 | $Z$ | 1 | 312.817 |
| 09 | $Z$ | 1 | 317.897 |
| 09 | $Z$ | 1 | 318.437 |
| 09 | $Z$ | 1 | 323.282 |
| 09 | $Z$ | 1 | 327.409 |
| 09 | $Z$ | 1 | 328.377 |
| 09 | $Z$ | 1 | 334.312 |
| 09 | $Z$ | 1 | 338.998 |
| 09 | $Z$ | 1 | 348.377 |
| 09 | $Z$ | 1 | 348.893 |
| 09 | $Z$ | 1 | 364.453 |
| 09 | $Z$ | 1 | 384.453 |
| 09 | $Z$ | 1 | 388.998 |
| 09 | $Z$ | 1 | 550.000 |

## DRIVER ASSEMBLY

Lower Ext
Lower Blanket Fuel Region
14 DEPB NA23I 0.000761778
14 DEPB U235N 0.000044937 U 238 N 0.014745338
14 DEPB FE__R $0.010127125 N I \_R \quad 0.001628561 C R \_R 0.002604296$
Above Lower Blanket Fuel Region
14 DEPBT NA23I 0.012141076
14 DEPBT FE__R 0.030510065 NI__R 0.004906379 CR__R 0.007845981
Below Lower Blanket Fuel Region
14 DEPBB NA23I 0.007284646
14 DEPBB FE__R 0.042714091 NI__R $0.006868930 C R \_$R 0.010984373
MID Section
Fuel Region
14 FUEL NA23I 0.001379298
14 FUEL FS__H 0.001783781U235N 0.006815427U238N 0.007266792
14 FUEL FE__R 0.012225156 NI__R $0.001965949 C R \_R 0.003143826$
Above Fuel region
14 FUELT NA23I 0.012204748
14 FUELT FE__R 0.030350 NI__R $0.004880648 C R \_R 0.007804833$
Below Fuel region
14 FUELB NA23I 0.011013176
14 FUELB FE__R $0.033344434 N I \_$R $0.005362179 C R \_$R 0.008574868


14 DEPTB FE__R 0.03051006 NI__R 0.00490638 CR__R 0.00784598 ss reflector very bottom piece
14 REFL FE__R 0.06102013 NI__R 0.00981276 CR__R 0.01569196 14 REFL NA23I 0.02428215

## EMPTY DRIVER ASSEMBLY

Lower Ext
Lower Blanket Fuel Region
14 EDEPB NA23I 0.000761778
14 DEPB U235N 0.000044937U238N 0.014745338
14 EDEPB FE__R $0.010127125 N I \_$R $0.001628561 C R \_$R 0.002604296
Above Lower Blanket Fuel Region
14 EDEPBTNA23I 0.012141076
14 EDEPBTFE__R $0.030510065 N I \_$R 0.004906379 CR__R 0.007845981
Below Lower Blanket Fuel Region
14 EDEPBBNA23I 0.007284646
14 EDEPBBFE__R 0.042714091 NI__R $0.006868930 C R \_R 0.010984373$
MID Section
Fuel Region
14 EFUEL NA23I 0.001379298
14 FUEL FS__H 0.001783781 U 235 N 0.006815427 U 238 N 0.007266792
14 EFUEL FE__R 0.012225156 NI__R $0.001965949 C R \_\_R 0.003143826$
Above Fuel region
14 EFUELTNA23I 0.012204748
14 EFUELTFE_R 0.030350 NI__R $0.004880648 C R \_R 0.007804833$
Below Fuel region
14 EFUELBNA23I 0.011013176
14 EFUELBFE__R 0.033344434 NI__R $0.005362179 C R \_$R 0.008574868
Upper Ext
Upper Blanket Fuel Region
14 EDEPT NA23I 0.012660584
14 DEPT U235N 0.000044937U238N 0.014745338
14 EDEPT FE__R $0.010127125 N I \_\_R 0.001628561 C R \_\_R 0.002604296$
Above Upper Blanket Fuel Region
14 EDEPTTNA23I 0.022611307
14 EDEPTTFE__R $0.004194342 N I \_R \quad 0.000674500 C R \_R \quad 0.001078619$
Below Upper Blanket Fuel Region
14 EDEPTBNA23I 0.012141080
14 EDEPTBFE__R 0.03051006 NI__R 0.00490638 CR__R 0.00784598
ss reflector very bottom piece
14 REFL FE__R 0.06102013 NI__R 0.00981276 CR__R 0.01569196 14 REFL NA23I 0.02428215

## NaTURAL URANIUM DRIVER ASSEMBLY

Lower Ext
Lower Blanket Fuel Region
14 NDEPB NA23I 0.012660584
14 NDEPB U235N 0.000044937 U 238 N 0.014745338
14 NDEPB FE_R $0.010127125 N I \_R \quad 0.001628561 C R \_R \quad 0.002604296$
Above Lower Blanket Fuel Region
14 NDEPBTNA23I 0.012141076
14 NDEPBTFE__R $0.030510065 N I \_$R $0.004906379 C R \_$R 0.007845981


Just sodium above and below ALSO AROUND BLANKET REGION

## 14 SODI NA23I 0.02428215

```
    INNER BLANKET REGION MATERIALS
    Fuel Region
14 IBFR NA23I 0.001708712
14 IBFR U235N 0.000059186U238N 0.029160810
14 IBFR FE__R 0.011069454NI__R 0.001780099CR__R 0.002846625
    Above Fuel Region
14 IBFRT NA23I 0.007155620
14 IBFRT FE__R 0.022825034NI__R 0.003670535CR__R 0.005869695
    TOP of the INNER BLANKET
14 IBT NA23I 0.007284646
14 IBT FE__R 0.042714091NI__R 0.006868930CR__R 0.010984373
```


## EMPTY INNER BLANKET



ENRICHED INNER BLANKET REGION MATERIALS

```
        Fuel Region
14 IBEFR NA23B 0.001708712
14 IBEFR U235B 0.001769759U238B 0.027471844
14 IBEFR FE__B 0.011069454NI__B 0.001780099CR__B 0.002846625
```

OUTER BLANKET REGION MATERIAL
Fuel Region
14 OBFR NA23I $0.001708712 \mathrm{U} 235 \mathrm{~N} \quad 0.000059186 \mathrm{U} 238 \mathrm{~N} \quad 0.029160810$
CONTROL ROD
Fuel Region
14 CR NA23I 0.006707 U235N 0.004568583 U 238 N 0.004871146
14 CR FS__H 0.001195721
14 CR FE__R $0.013057054 N I \_$R $0.002099728 C R \_$R 0.003357757
Above Fuel region
14 CRT NA23I 0.014251475
14 CRT FE__R $0.025206714 N I \_$R $0.004053537 C R \_R 0.006482169$
Below Fuel region
14 CRB NA23I 0.013452728
14 CRB FE__R 0.027213933NI__R 0.004376322CR_R 0.006998346
Void section above fuel
14 VOID NA23I 0.021228481
14 VOID FE__R 0.007673761 NI__R $0.001234031 C R \_$R 0.001973387
Poison instead of VOID
14 B4C FE__X 1.35683E-02NA23X 1.20403E-02CR_X 3.98487E-03
14 B4C NI_X 1.93593E-03B10_X 7.81500E-03C__X 9.76875E-03
14 B4C B11_X 3.12609E-02
Reflector above Void
14 CRRF NA23I 0.021228481
14 CRRF FE__R 0.007673761 NI__R $0.001234031 C R \_$R 0.001973387
Very top piece
14 CRTP NA23I 0.021853937
14 CRTP FE__R $0.006102013 N I \_$R $0.000981276 C R \_$R 0.001569196
Very bottom piece
14 CRBP NA23I 0.004856430
14 CRBP FE__R $0.048816104 N I \_$R $0.007850206 C R \_$R 0.012553569
Reflector on top and bottom
14 OREF FE__R 0.488161040 NI__R $0.078502060 C R \_$R 0.125535690
SOURCE ROD
14 SOUR NA23I 0.001709000
14 SOUR FE__R $0.011069454 N I \_$R $0.001780099 C R \_$R 0.002846625

DRIVER ASSEMBLY NAMING

15 DEPBB FR1BB

| 15 | DEPB FR1B |
| :---: | :---: |
| 15 | DEPBT FR1BT |
| 15 | FUELB FR1FB |
| 15 | FUEL FR1F |
| 15 | FUELT FR1FT |
| 15 | DEPTB FR1TB |
| 15 | DEPT FR1T |
| 15 | DEPTT FR1TT |
| 15 | DEPBB R2BB |
| 15 | DEPB R2B |
| 15 | DEPBT R2BT |
| 15 | FUELB R2FB |
| 15 | FUEL R2F |
| 15 | FUELT R2FT |
| 15 | DEPTB R2TB |
| 15 | DEPT R2T |
| 15 | DEPTT R2TT |
| 15 | DEPBB R3BB |
| 15 | DEPB R3B |
| 15 | DEPBT R3BT |
| 15 | FUELB R3FB |
| 15 | FUEL R3F |
| 15 | FUELT R3FT |
| 15 | DEPTB R3TB |
| 15 | DEPT R3T |
| 15 | DEPTT R3TT |
| 15 | EDEPBBR4BB |
| 15 | EDEPB R4B |
| 15 | EDEPBTR4BT |
| 15 | EFUELBR4FB |
| 15 | EFUEL R4F |
| 15 | EFUELTR4FT |
| 15 | EDEPTBR4TB |
| 15 | EDEPT R4T |
| 15 | EDEPTTR4TT |
| 15 | DEPBB FR4BB |
| 15 | DEPB FR4B |
| 15 | DEPBT FR4BT |
| 15 | FUELB FR4FB |
| 15 | FUEL FR4F |
| 15 | FUELT FR4FT |
| 15 | DEPTB FR4TB |
| 15 | DEPT FR4T |
| 15 | DEPTT FR4TT |
| 15 | NDEPBBNR4BB |
| 15 | NDEPB NR4B |
| 15 | NDEPBTNR4BT |
| 15 | NFUELBNR4FB |
| 15 | NFUEL NR4F |
| 15 | NFUELTNR4FT |
| 15 | NDEPTBNR4TB |

```
    15 NDEPT NR4T
    15 NDEPTTNR4TT
    NDEPBBR5BB
    NDEPB R5B
    NDEPBTR5BT
    NFUELBR5FB
    NFUEL R5F
        NFUELTR5FT
        NDEPTBR5TB
        NDEPT R5T
        NDEPTTR5TT
        DEPBB R5BB
        DEPB R5B
        DEPBT R5BT
        FUELB R5FB
        FUEL R5F
        FUELT R5FT
        DEPTB R5TB
        DEPT R5T
        DEPTT R5TT
        REFL BOT
        SODI BOTS
        SODI TOPS
    INNER BLANKET ASSEMBLY NAMING
        DEPBB R6BB
        IBFR R6F
        IBFRT R6FT
        IBT R6T
        DEPBB FR6BB
        IBEFR FR6F
        IBFRT FR6FT
        IBT FR6T
        DEPBB R7BB
        IBEFR R7F
        IBFRT R7FT
        IBT R7T
        EIBFR R6DET
        EIBFR R7DET
    SODIUM AROUND BLANKET REGION
15 SODI EMPT
    OUTER BLANKET ASSEMBLY NAMING
15 DEPBB R8BB
OBFR R8F
OBFRT R8FT
    OBT R8T
    DEPBB R9BB
```

| 15 | OBFR R9F |
| :--- | :--- |
| 15 | OBFRT R9FT |
| 15 | OBT R9T |
| 15 | DEPBB R10BB |
| 15 | OBFR R10F |
| 15 | OBFRT R10FT |
| 15 | OBT R10T |
| 15 | DEPBB R11BB |
| 15 | OBFR R11F |
| 15 | OBFRT R11FT |
| 15 | OBT R11T |
| 15 | DEPBB R12BB |
| 15 | OBFR R12F |
| 15 | OBFRT R12FT |
| 15 | OBT R12T |
| 15 | DEPBB R13BB |
| 15 | OBFR R13F |
| 15 | OBFRT R13FT |
| 15 | OBT R13T |
| 15 | DEPBB R14BB |
| 15 | OBFR R14F |
| 15 | OBFRT R14FT |
| 15 | OBT R14T |
| 15 | DEPBB R15BB |
| 15 | CRBP CRBPB |
| 15 | CRB CRBB |
| 15 | CR CRB |
| 15 | CRT CRTB |
| 15 | OBFR R15F |
| 15 | OBFRT R15FT |
| 15 | OBT R15T |
| 15 | DEPBB R16BB |
| 15 | CRBP CRBPA |
| 15 | CRB CRBA |
| 15 | CR CRA |
| 15 | CRT CRTA |
| 15 | VOID VOIDA |
| 15 | CRRF CRRFA |
| 15 | OBFR R16F |
| 15 | OBFRT R16FT |
| 15 | OBT R16T |
| 15 | OBFR R11DET |
| 15 OBFR R13DET |  |
| 15 ORTPA |  |
| 15 |  |


| 15 | VOID VOIDB |
| :--- | :--- |
| 15 | CRRF CRRFB |
| 15 | CRTP CRTPB |
| 15 | CRBP CRBPC |
| 15 | CRB CRBC |
| 15 | CR CRC |
| 15 | CRT CRTC |
| 15 | VOID VOIDC |
| 15 | CRRF CRRFC |
| 15 | CRTP CRTPC |
| 15 | CRBP CRBPD |
| 15 | CRB CRBD |
| 15 | CR CRD |
| 15 | CRT CRTD |
| 15 | VOID VOIDD |
| 15 | CRRF CRRFD |
| 15 | CRTP CRTPD |
| 15 | CRBP CRBPE |
| 15 | CRB CRBE |
| 15 | CR CRE |
| 15 | CRT CRTE |
| 15 | VOID VOIDE |
| 15 | CRRF CRRFE |
| 15 | CRTP CRTPE |
| 15 | CRBP CRBPF |
| 15 | CRB CRBF |
| 15 | CR CRF |
| 15 | CRBB CRBI |
| 15 | CR CRI |
| 15 | CRT CRTI |
| 15 | CRT CRTF |
| 15 | VOID VOIDF |
| 15 | CRRF CRRFF |
| 15 | CRTP CRTPF |
| 15 | CRBP CRBPH |
| 15 | CRB CRBH |
| 15 | CR CRH |
| 15 | CRT CRTH |
| 15 | VOID VOIDH |
| 15 | CRRF CRRFH |
| 15 | CRBP CRBPG |
| 15 | CRB CRBG |
| 15 | CR CRG |
| 15 | CRT CRTG |
| 15 | B4C POISN |
| 15 | CRRF CRRFG |
| 15 | CRTP CRTPG |
| 15 |  |

```
VOID VOIDI
CRRF CRRFI
CRTP CRTPI
CRBP CRBPJ
CRB CRBJ
CR CRJ
CRT CRTJ
VOID VOIDJ
CRRF CRRFJ
CRTP CRTPJ
    CRBP CRBPK
    CRB CRBK
    CR CRK
    CRT CRTK
    VOID VOIDK
    CRRF CRRFK
    CRTP CRTPK
    CRBP CRBPL
    CRB CRBL
    CR CRL
    CRT CRTL
    VOID VOIDL
    CRRF CRRFL
    CRTP CRTPL
    OREF OREF
    OREF OREF8
    OREF OREF9
    OREF OREF10
    OREF OREF11
    OREF OREF12
    OREF OREF13
    OREF OREF14
    OREF OREF15
    OREF OREF16
    OREF OREF17
    OREF OREF18
    OREF OREF19
    OREF OREF20
    OREF OREF21
    OREF OREF22
    OREF OREF23
    OREF OREF24
    OREF OREF25
    SOUR SOURC1
    SOUR SOURB
    SOUR SOURT
19 SOURC1 1 662.517546E+07
19 SOURC1 1 33 1.0
29 5.80898 25 3
```


## DRIVER REGION

| 30 | OREF | 01 | 0.0 | 60.000 |
| :---: | :---: | :---: | :---: | :---: |
| 30 | BOTS | 01 | 60.000 | 120.000 |
| 30 | BOT | 01 | 120.000 | 172.070 |
| 30 | FR1BB | 01 | 172.070 | 178.737 |
| 30 | FR1B | 01 | 178.737 | 224.457 |
| 30 | FR1BT | 01 | 224.457 | 232.553 |
| 30 | FR1FB | 01 | 232.553 | 234.458 |
| 30 | FR1F | 01 | 234.458 | 270.577 |
| 30 | FR1FT | 01 | 270.577 | 278.527 |
| 30 | FR1TB | 01 | 278.527 | 281.689 |
| 30 | FR1T | 01 | 281.689 | 327.409 |
| 30 | FR1TT | 01 | 327.409 | 338.998 |
| 30 | TOPS | 01 | 338.998 | 388.998 |
| 30 | OREF | 01 | 388.998 | 550.000 |
|  |  |  |  |  |
| 30 | OREF | 02 | 0.0 | 60.000 |
| 30 | BOTS | 02 | 60.000 | 120.000 |
| 30 | BOT | 02 | 120.000 | 172.070 |
| 30 | R2BB | 02 | 172.070 | 178.737 |
| 30 | R2B | 02 | 178.737 | 224.457 |
| 30 | R2BT | 02 | 224.457 | 232.553 |
| 30 | R2FB | 02 | 232.553 | 234.458 |
| 30 | R2F | 02 | 234.458 | 270.577 |
| 30 | R2FT | 02 | 270.577 | 278.527 |
| 30 | R2TB | 02 | 278.527 | 281.689 |
| 30 | R2T | 02 | 281.689 | 327.409 |
| 30 | R2TT | 02 | 327.409 | 338.998 |
| 30 | TOPS | 02 | 338.998 | 388.998 |
| 30 | OREF | 02 | 388.998 | 550.000 |
|  |  |  |  |  |
| 30 | OREF | 03 | 0.0 | 60.000 |
| 30 | BOTS | 03 | 60.000 | 120.000 |
| 30 | BOT | 03 | 120.000 | 172.070 |
| 30 | R3BB | 03 | 172.070 | 178.737 |
| 30 | R3B | 03 | 178.737 | 224.457 |
| 30 | R3BT | 03 | 224.457 | 232.553 |
| 30 | R3FB | 03 | 232.553 | 234.458 |
| 30 | R3F | 03 | 234.458 | 270.577 |
| 30 | R3FT | 03 | 270.577 | 278.527 |
| 30 | R3TB | 03 | 278.527 | 281.689 |
| 30 | R3T | 03 | 281.689 | 327.409 |
| 30 | R3TT | 03 | 327.409 | 338.998 |
| 30 | TOPS | 03 | 338.998 | 388.998 |
| 30 | OREF | 03 | 388.998 | 550.000 |
|  | 03 |  |  |  |
| 3 |  |  |  |  |

Safety

| 30 | OREF | 03 | 1 | 1 | 0.0 | 60.000 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | BOTS | 03 | 1 | 1 | 60.000 | 157.504 |
| 30 | CRBPA | 03 | 1 | 1 | 157.504 | 231.918 |
| 30 | CRBA | 03 | 1 | 1 | 231.918 | 233.823 |
| 30 | CRA | 03 | 1 | 1 | 233.823 | 269.942 |
| 30 | CRTA | 03 | 1 | 1 | 269.942 | 277.892 |
| 30 | VOIDA | 03 | 1 | 1 | 277.892 | 317.897 |
| 30 | CRRFA | 03 | 1 | 1 | 317.897 | 348.377 |


| 30 | CRTPA 03 | 1 | 1 | 348.377 | 384.453 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | TOPS 03 | 1 | 1 | 384.453 | 388.998 |
| 30 | OREF 03 | 1 | 1 | 388.998 | 550.000 |
| 30 | OREF 03 | 2 | 6 | 0.0 | 60.000 |
| 30 | BOTS 03 | 2 | 6 | 60.000 | 120.000 |
| 30 | BOT 03 | 2 | 6 | 120.000 | 172.070 |
| 30 | R3BB 03 | 2 | 6 | 172.070 | 178.737 |
| 30 | R3B 03 | 2 | 6 | 178.737 | 224.457 |
| 30 | R3BT 03 | 2 | 6 | 224.457 | 232.553 |
| 30 | R3FB 03 | 2 | 6 | 232.553 | 234.458 |
| 30 | R3F 03 | 2 | 6 | 234.458 | 270.577 |
| 30 | R3FT 03 | 2 | 6 | 270.577 | 278.527 |
| 30 | R3TB 03 | 2 | 6 | 278.527 | 281.689 |
| 30 | R3T 03 | 2 | 6 | 281.689 | 327.409 |
| 30 | R3TT 03 | 2 | 6 | 327.409 | 338.998 |
| 30 | TOPS 03 | 2 | 6 | 338.998 | 388.998 |
| 30 | OREF 03 | 2 | 6 | 388.998 | 550.000 |
| 30 | OREF 03 | 7 | 7 | 0.0 | 60.000 |
| 30 | BOTS 03 | 7 | 7 | 60.000 | 157.504 |
| 30 | CRBPA 03 | 7 | 7 | 157.504 | 4231.918 |
| 30 | CRBA 03 | 7 | 7 | 231.918 | 233.823 |
| 30 | CRA 03 | 7 | 7 | 233.823 | 269.942 |
| 30 | CRTA 03 | 7 | 7 | 269.942 | 277.892 |
| 30 | VOIDA 03 | 7 | 7 | 277.892 | 2317.897 |
| 30 | CRRFA 03 | 7 | 7 | 317.897 | 348.377 |
| 30 | CRTPA 03 | 7 | 7 | 348.377 | 384.453 |
| 30 | TOPS 03 | 7 | 7 | 384.453 | 388.998 |
| 30 | OREF 03 | 7 | 7 | 388.998 | 550.000 |
| 30 | OREF 03 | 8 | 12 | 0.0 | 60.000 |
| 30 | BOTS 03 | 8 | 12 | 60.000 | 120.000 |
| 30 | BOT 03 | 8 | 12 | 120.000 | 172.070 |
| 30 | R3BB 03 | 8 | 12 | 172.070 | 178.737 |
| 30 | R3B 03 | 8 | 12 | 178.737 | 224.457 |
| 30 | R3BT 03 | 8 | 12 | 224.457 | 232.553 |
| 30 | R3FB 03 | 8 | 12 | 232.553 | 234.458 |
| 30 | R3F 03 | 8 | 12 | 234.458 | 270.577 |
| 30 | R3FT 03 | 8 | 12 | 270.577 | 278.527 |
| 30 | R3TB 03 | 8 | 12 | 278.527 | 281.689 |
| 30 | R3T 03 | 8 | 12 | 281.689 | 327.409 |
| 30 | R3TT 03 | 8 | 12 | 327.409 | 338.998 |
| 30 | TOPS 03 | 8 | 12 | 338.998 | 388.998 |
| 30 | OREF 03 | 8 | 12 | 388.998 | 550.000 |
| 30 | OREF 04 |  |  | 0.06 | 60.000 |
| 30 | BOTS 04 |  |  | 60.000 | 120.000 |
| 30 | BOT 04 |  |  | 120.000 | 172.070 |
| 30 | FR4BB 04 |  |  | 172.070 | 178.737 |
| 30 | FR4B 04 |  |  | 178.737 | 224.457 |
| 30 | FR4BT 04 |  |  | 224.457 | 232.553 |
| 30 | FR4FB 04 |  |  | 232.553 | 234.458 |
| 30 | FR4F 04 |  |  | 234.458 | 270.577 |
| 30 | FR4FT 04 |  |  | 270.577 | 278.527 |
| 30 | FR4TB 04 |  |  | 278.527 | 281.689 |


| 30 | FR4T | 04 |  | 281.689 | 327.409 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | FR4TT | 04 |  | 327.409 | 338.998 |
| 30 | TOPS | 04 |  | 338.998 | 388.998 |
| 30 | OREF | 04 |  | 388.998 | 550.000 |
| 30 | OREF | 05 |  | 0.06 | 60.000 |
| 30 | BOTS | 05 | 1 | 60.000 | 157.504 |
| 30 | CRBPA | 05 | 1 | 157.504 | $4 \quad 231.918$ |
| 30 | CRBA | 05 | 1 | 231.918 | 233.823 |
| 30 | CRA | 05 | 11 | 233.823 | 269.942 |
| 30 | CRTA | 05 | 11 | 269.942 | 277.892 |
| 30 | VOIDA | 05 | 1 | 277.892 | 2317.897 |
| 30 | CRRFA | 05 | , | 317.897 | 348.377 |
| 30 | CRTPA | 05 | 1 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 11 | 384.453 | 388.998 |
| 30 | OREF | 05 |  | 388.998 | 550.000 |
| 30 | BOTS | 05 | 22 | 60.000 | 120.000 |
| 30 | BOT | 05 | 22 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 22 | 172.070 | 178.737 |
| 30 | R5B | 05 | 22 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 22 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 22 | 232.553 | 234.458 |
| 30 | R5F | 05 | 22 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 22 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 22 | 278.527 | 281.689 |
| 30 | R5T | 05 | 22 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 22 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 22 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 33 | 60.000 | 157.504 |
| 30 | CRBPB | 05 | 3 | 157.504 | 4231.918 |
| 30 | CRBB | 05 | 3 | 231.918 | 233.823 |
| 30 | CRB | 05 | 33 | 233.823 | 269.942 |
| 30 | CRTB | 05 | 33 | 269.942 | 277.892 |
| 30 | VOIDB | 05 | 3 | 277.892 | 317.897 |
| 30 | CRRFB | 05 | 3 | $3 \quad 317.897$ | 348.377 |
| 30 | CRTPB | 05 | 3 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 33 | 384.453 | 388.998 |
| 30 | BOTS | 05 | $4 \quad 4$ | 60.000 | 120.000 |
| 30 | BOT | 05 | 44 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 44 | 172.070 | 178.737 |
| 30 | R5B | 05 | 44 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 44 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 44 | 232.553 | 234.458 |
| 30 | R5F | 05 | 44 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 44 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 44 | 278.527 | 281.689 |
| 30 | R5T | 05 | 44 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 44 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 4 | 338.998 | 388.998 |

Control rod 3-12 fully up
30 BOTS $\quad 05 \quad 5 \quad 5 \quad 60.000 \quad 157.504$

| 30 | CRBPC 05 | 5 | 5 | 157.504 | 231.918 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | CRBC 05 | 5 | 5 | 231.918 | 233.823 |
| 30 | CRC 05 | 5 | 5 | 233.823 | 269.942 |
| 30 | CRTC 05 | 5 | 5 | 269.942 | 277.892 |
| 30 | VOIDC 05 | 5 | 5 | 277.892 | 317.897 |
| 30 | CRRFC 05 | 5 | 5 | 317.897 | 348.377 |
| 30 | CRTPC 05 | 5 | 5 | 348.377 | 384.453 |
| 30 | TOPS 05 | 5 | 5 | 384.453 | 388.998 |
| 30 | BOTS 05 | 6 | 6 | 60.000 | 120.000 |
| 30 | BOT 05 | 6 | 6 | 120.000 | 172.070 |
| 30 | R5BB 05 | 6 | 6 | 172.070 | 178.737 |
| 30 | R5B 05 |  | 6 | 178.737 | 224.457 |
| 30 | R5BT 05 | 6 | 6 | 224.457 | 232.553 |
| 30 | R5FB 05 | 6 | 6 | 232.553 | 234.458 |
| 30 | R5F 05 |  | 6 | 234.458 | 270.577 |
| 30 | R5FT 05 | 6 | 6 | 270.577 | 278.527 |
| 30 | R5TB 05 | 6 | 6 | 278.527 | 281.689 |
| 30 | R5T 05 |  | 6 | 281.689 | 327.409 |
| 30 | R5TT 05 | 6 | 6 | 327.409 | 338.998 |
| 30 | TOPS 05 | 6 | 6 | 338.998 | 388.998 |
| 30 | BOTS 05 | 7 | 7 | 60.000 | 157.504 |
| 30 | CRBPD 05 | 7 | 7 | 157.504 | 231.918 |
| 30 | CRBD 05 | 7 | 7 | 231.918 | 233.823 |
| 30 | CRD 05 | 7 | 7 | 233.823 | 269.942 |
| 30 | CRTD 05 | 7 | 7 | 269.942 | 277.892 |
| 30 | VOIDD 05 | 7 | 7 | 277.892 | 317.897 |
| 30 | CRRFD 05 | 7 | 7 | 317.897 | 348.377 |
| 30 | CRTPD 05 | 7 | 7 | 348.377 | 384.453 |
| 30 | TOPS 05 | 7 | 7 | 384.453 | 388.998 |
| 30 | BOTS 05 | 8 | 8 | 60.000 | 120.000 |
| 30 | BOT 05 | 8 | 8 | 120.000 | 172.070 |
| 30 | R5BB 05 | 8 | 8 | 172.070 | 178.737 |
| 30 | R5B 05 | 8 | 8 | 178.737 | 224.457 |
| 30 | R5BT 05 | 8 | 8 | 224.457 | 232.553 |
| 30 | R5FB 05 | 8 | 8 | 232.553 | 234.458 |
| 30 | R5F 05 | 8 | 8 | 234.458 | 270.577 |
| 30 | R5FT 05 | 8 | 8 | 270.577 | 278.527 |
| 30 | R5TB 05 | 8 | 8 | 278.527 | 281.689 |
| 30 | R5T 05 | 8 | 8 | 281.689 | 327.409 |
| 30 | R5TT 05 | 8 | 8 | 327.409 | 338.998 |
| 30 | TOPS 05 | 8 | 8 | 338.998 | 388.998 |
| 30 | BOTS 05 | 9 | 9 | 60.000 | 157.504 |
| 30 | CRBPE 05 | 9 | 9 | 157.504 | 231.918 |
| 30 | CRBE 05 | 9 | 9 | 231.918 | 233.823 |
| 30 | CRE 05 | 9 | 9 | 233.823 | 269.942 |
| 30 | CRTE 05 | 9 | 9 | 269.942 | 277.892 |
| 30 | VOIDE 05 | 9 | 9 | 277.892 | 317.897 |
| 30 | CRRFE 05 | 9 | 9 | 317.897 | 348.377 |
| 30 | CRTPE 05 | 9 | 9 | 348.377 | 384.453 |
| 30 | TOPS 05 | 9 | 9 | 384.453 | 388.998 |
| 30 | BOTS 05 | 10 | 10 | 60.000 | 120.000 |


| 30 | BOT | 05 | 10 | 10 | 120.000 | 172.070 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | R5BB | 05 | 10 | 10 | 172.070 | 178.737 |
| 30 | R5B | 05 | 10 | 10 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 10 | 10 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 10 | 10 | 232.553 | 234.458 |
| 30 | R5F | 05 | 10 | 10 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 10 | 10 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 10 | 10 | 278.527 | 281.689 |
| 30 | R5T | 05 | 10 | 10 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 10 | 10 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 10 | 10 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 11 | 11 | 60.000 | 157.504 |
| 30 | CRBPF | 05 | 11 | 11 | 157.504 | 231.918 |
| 30 | CRBF | 05 | 11 | 11 | 231.918 | 233.823 |
| 30 | CRF | 05 | 11 | 11 | 233.823 | 269.942 |
| 30 | CRTF | 05 | 11 | 11 | 269.942 | 277.892 |
| 30 | VOIDF | 05 | 11 | 11 | 277.892 | 317.897 |
| 30 | CRRFF | 05 | 11 | 11 | 317.897 | 348.377 |
| 30 | CRTPF | 05 | 11 | 11 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 11 | 11 | 384.453 | 388.998 |
| 30 | BOTS | 05 | 12 | 12 | 60. | .000 |
| 30 | BOT | 05 | 12 | 12 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 12 | 12 | 172.070 | 178.737 |
| 30 | R5B | 05 | 12 | 12 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 12 | 12 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 12 | 12 | 232.553 | 234.458 |
| 30 | R5F | 05 | 12 | 12 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 12 | 12 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 12 | 12 | 278.527 | 281.689 |
| 30 | R5T | 05 | 12 | 12 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 12 | 12 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 12 | 12 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 13 | 13 | 60.000 | 157.504 |
| 30 | CRBPG | 05 | 13 | 13 | 157.504 | 231.918 |
| 30 | CRBG | 05 | 13 | 13 | 231.918 | 233.823 |
| 30 | CRG | 05 | 13 | 13 | 233.823 | 269.942 |
| 30 | CRTG | 05 | 13 | 13 | 269.942 | 287.722 |
| 30 | POISN | 05 | 13 | 13 | 287.722 | 323.282 |
| 30 | CRRFG | 05 | 13 | 13 | 323.282 | 348.377 |
| 30 | CRTPG | 05 | 13 | 13 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 13 | 13 | 384.453 | 388.998 |
| 30 | BOTS | 05 | 14 | 14 | 60.000 | 120.000 |
| 30 | BOT | 05 | 14 | 14 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 14 | 14 | 172.070 | 178.737 |
| 30 | R5B | 05 | 14 | 14 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 14 | 14 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 14 | 14 | 232.553 | 234.458 |
| 30 | R5F | 05 | 14 | 14 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 14 | 14 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 14 | 14 | 278.527 | 281.689 |
| 30 | R5T | 05 | 14 | 14 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 14 | 14 | 327.409 | 338.998 |


| 30 | TOPS | 05 | 14 | 14 | 338.998 | 388.998 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | BOTS | 05 | 15 | 15 | 60.000 | 157.504 |
| 30 | CRBPH | 05 | 15 | 15 | 157.504 | 231.918 |
| 30 | CRBH | 05 | 15 | 15 | 231.918 | 233.823 |
| 30 | CRH | 05 | 15 | 15 | 233.823 | 269.942 |
| 30 | CRTH | 05 | 15 | 15 | 269.942 | 277.892 |
| 30 | VOIDH | 05 | 15 | 15 | 277.892 | 317.897 |
| 30 | CRRFH | 05 | 15 | 15 | 317.897 | 348.377 |
| 30 | CRTPH | 05 | 15 | 15 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 15 | 15 | 384.453 | 388.998 |
| 30 | BOTS | 05 | 16 | 16 | 60.000 | 120.000 |
| 30 | BOT | 05 | 16 | 16 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 16 | 16 | 172.070 | 178.737 |
| 30 | R5B | 05 | 16 | 16 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 16 | 16 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 16 | 16 | 232.553 | 234.458 |
| 30 | R5F | 05 | 16 | 16 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 16 | 16 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 16 | 16 | 278.527 | 281.689 |
| 30 | R5T | 05 | 16 | 16 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 16 | 16 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 16 | 16 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 17 | 17 | 60.000 | 157.504 |
| 30 | CRBPI | 05 | 17 | 17 | 157.504 | 231.918 |
| 30 | CRBI | 05 | 17 | 17 | 231.918 | 233.823 |
| 30 | CRI | 05 | 17 | 17 | 233.823 | 269.942 |
| 30 | CRTI | 05 | 17 | 17 | 269.942 | 277.892 |
| 30 | VOIDI | 05 | 17 | 17 | 277.892 | 317.897 |
| 30 | CRRFI | 05 | 17 | 17 | 317.897 | 348.377 |
| 30 | CRTPI | 05 | 17 | 17 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 17 | 17 | 384.453 | 388.998 |
| 30 | BOTS | 05 | 18 | 18 | 60.000 | 120.000 |
| 30 | BOT | 05 | 18 | 18 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 18 | 18 | 172.070 | 178.737 |
| 30 | R5B | 05 | 18 | 18 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 18 | 18 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 18 | 18 | 232.553 | 234.458 |
| 30 | R5F | 05 | 18 | 18 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 18 | 18 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 18 | 18 | 278.527 | 281.689 |
| 30 | R5T | 05 | 18 | 18 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 18 | 18 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 18 | 18 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 19 | 19 | 60.000 | 157.504 |
| 30 | CRBPJ | 05 | 19 | 19 | 157.504 | 231.918 |
| 30 | CRBJ | 05 | 19 | 19 | 231.918 | 233.823 |
| 30 | CRJ | 05 | 19 | 19 | 233.823 | 269.942 |
| 30 | CRTJ | 05 | 19 | 19 | 269.942 | 277.892 |
| 30 | VOIDJ | 05 | 19 | 19 | 277.892 | 317.897 |
| 30 | CRRFJ | 05 | 19 | 19 | 317.897 | 348.377 |
| 30 | CRTPJ | 05 | 19 | 19 | 348.377 | 384.453 |


| 30 | TOPS | 05 | 19 | 19 | 384.453 | 388.998 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | BOTS | 05 | 20 | 20 | 60.000 | 120.000 |
| 30 | BOT | 05 | 20 | 20 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 20 | 20 | 172.070 | 178.737 |
| 30 | R5B | 05 | 20 | 20 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 20 | 20 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 20 | 20 | 232.553 | 234.458 |
| 30 | R5F | 05 | 20 | 20 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 20 | 20 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 20 | 20 | 278.527 | 281.689 |
| 30 | R5T | 05 | 20 | 20 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 20 | 20 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 20 | 20 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 21 | 21 | 60.000 | 157.504 |
| 30 | CRBPK | 05 | 21 | 21 | 157.504 | 231.918 |
| 30 | CRBK | 05 | 21 | 21 | 231.918 | 233.823 |
| 30 | CRK | 05 | 21 | 21 | 233.823 | 269.942 |
| 30 | CRTK | 05 | 21 | 21 | 269.942 | 277.892 |
| 30 | VOIDK | 05 | 21 | 21 | 277.892 | 317.897 |
| 30 | CRRFK | 05 | 21 | 21 | 317.897 | 348.377 |
| 30 | CRTPK | 05 | 21 | 21 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 21 | 21 | 384.453 | 388.998 |
| 30 | BOTS | 05 | 22 | 22 | 60.000 | 120.000 |
| 30 | BOT | 05 | 22 | 22 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 22 | 22 | 172.070 | 178.737 |
| 30 | R5B | 05 | 22 | 22 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 22 | 22 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 22 | 22 | 232.553 | 234.458 |
| 30 | R5F | 05 | 22 | 22 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 22 | 22 | 270.577 | 278.527 |
| 30 | R5TB | 05 | 22 | 22 | 278.527 | 281.689 |
| 30 | R5T | 05 | 22 | 22 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 22 | 22 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 22 | 22 | 338.998 | 388.998 |
| 30 | BOTS | 05 | 23 | 23 | 60.000 | 157.504 |
| 30 | CRBPL | 05 | 23 | 23 | 157.504 | 231.918 |
| 30 | CRBL | 05 | 23 | 23 | 231.918 | 233.823 |
| 30 | CRL | 05 | 23 | 23 | 233.823 | 269.942 |
| 30 | CRTL | 05 | 23 | 23 | 269.942 | 277.892 |
| 30 | VOIDL | 05 | 23 | 23 | 277.892 | 317.897 |
| 30 | CRRFL | 05 | 23 | 23 | 317.897 | 348.377 |
| 30 | CRTPL | 05 | 23 | 23 | 348.377 | 384.453 |
| 30 | TOPS | 05 | 23 | 23 | 384.453 | 388.998 |
| 30 | BOTS | 05 | 24 | 24 | 60.000 | 120.000 |
| 30 | BOT | 05 | 24 | 24 | 120.000 | 172.070 |
| 30 | R5BB | 05 | 24 | 24 | 172.070 | 178.737 |
| 30 | R5B | 05 | 24 | 24 | 178.737 | 224.457 |
| 30 | R5BT | 05 | 24 | 24 | 224.457 | 232.553 |
| 30 | R5FB | 05 | 24 | 24 | 232.553 | 234.458 |
| 30 | R5F | 05 | 24 | 24 | 234.458 | 270.577 |
| 30 | R5FT | 05 | 24 | 24 | 270.577 | 278.527 |


| 30 | R5TB | 05 | 24 | 24 | 278.527 | 281.689 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | R5T | 05 | 24 | 24 | 281.689 | 327.409 |
| 30 | R5TT | 05 | 24 | 24 | 327.409 | 338.998 |
| 30 | TOPS | 05 | 24 | 24 | 338.998 | 388.998 |

## INNER BLANKET REGION

|  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | OREF | 06 | 1 | 5 | 0.0 | 60.000 |
| 30 | OREF | 06 | 1 | 5 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 1 | 5 | 60.000 | 120.000 |
| 30 | BOT | 06 | 1 | 5 | 120.000 | 172.070 |
| 30 | FR6BB | 06 | 1 | 5 | 172.070 | 178.737 |
| 30 | FR6F | 06 | 1 | 5 | 178.737 | 318.437 |
| 30 | FR6FT | 06 | 1 | 5 | 318.437 | 334.312 |
| 30 | FR6T | 06 | 1 | 5 | 334.312 | 338.998 |
| 30 | TOPS | 06 | 1 | 5 | 338.998 | 388.998 |
|  |  |  |  |  |  |  |
| 30 | OREF | 06 | 6 | 6 | 0.0 | 60.000 |
| 30 | OREF | 06 | 6 | 6 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 6 | 6 | 60.000 | 120.000 |
| 30 | BOT | 06 | 6 | 6 | 120.000 | 172.070 |
| 30 | R6BB | 06 | 6 | 6 | 172.070 | 178.737 |
| 30 | R6F | 06 | 6 | 6 | 178.737 | 318.437 |
| 30 | R6FT | 06 | 6 | 6 | 318.437 | 334.312 |
| 30 | R6T | 06 | 6 | 6 | 334.312 | 338.998 |
| 30 | TOPS | 06 | 6 | 6 | 338.998 | 388.998 |
| 7 |  |  |  |  |  |  |
| 30 | OREF | 06 | 7 | 10 | 0.0 | 60.000 |
| 30 | OREF | 06 | 7 | 10 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 7 | 10 | 60.000 | 120.000 |
| 30 | BOT | 06 | 7 | 10 | 120.000 | 172.070 |
| 30 | FR6BB | 06 | 7 | 10 | 172.070 | 178.737 |
| 30 | FR6F | 06 | 7 | 10 | 178.737 | 318.437 |
| 30 | FR6FT | 06 | 7 | 10 | 318.437 | 334.312 |
| 30 | FR6T | 06 | 7 | 10 | 334.312 | 338.998 |
| 30 | TOPS | 06 | 7 | 10 | 338.998 | 388.998 |
| 30 |  |  |  |  |  |  |
| 30 | OREF | 06 | 11 | 11 | 0.0 | 60.000 |
| 30 | OREF | 06 | 11 | 11 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 11 | 11 | 60.000 | 120.000 |
| 30 | BOT | 06 | 11 | 11 | 120.000 | 172.070 |
| 30 | R6BB | 06 | 11 | 11 | 172.070 | 178.737 |
| 30 | R6DET | 06 | 11 | 11 | 178.737 | 318.437 |
| 30 | R6FT | 06 | 11 | 11 | 318.437 | 334.312 |
| 30 | R6T | 06 | 11 | 11 | 334.312 | 338.998 |
| 30 | TOPS | 06 | 11 | 11 | 338.998 | 388.998 |
| 30 |  |  |  |  |  |  |
| 30 | OREF | 06 | 12 | 24 | 0.0 | 60.000 |
| 30 | OREF | 06 | 12 | 24 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 12 | 24 | 60.000 | 120.000 |
| 30 | BOT | 06 | 12 | 24 | 120.000 | 172.070 |
| 30 | FR6BB | 06 | 12 | 24 | 172.070 | 178.737 |
| 30 | FR6F | 06 | 12 | 24 | 178.737 | 318.437 |
| 30 | FR6FT | 06 | 12 | 24 | 318.437 | 334.312 |
| 30 | FR6T | 06 | 12 | 24 | 334.312 | 338.998 |
|  | TOPS | 06 | 12 | 24 | 338.998 | 388.998 |
| 3 |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |


| 30 | OREF | 06 | 25 | 26 | 0.0 | 60.000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | OREF | 06 | 25 | 26 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 25 | 26 | 60.000 | 120.000 |
| 30 | BOT | 06 | 25 | 26 | 120.000 | 172.070 |
| 30 | R6BB | 06 | 25 | 26 | 172.070 | 178.737 |
| 30 | R6F | 06 | 25 | 26 | 178.737 | 318.437 |
| 30 | R6FT | 06 | 25 | 26 | 318.437 | 334.312 |
| 30 | R6T | 06 | 25 | 26 | 334.312 | 338.998 |
| 30 | TOPS | 06 | 25 | 26 | 338.998 | 388.998 |
|  |  |  |  |  |  |  |
| 30 | OREF | 06 | 27 | 30 | 0.0 | 60.000 |
| 30 | OREF | 06 | 27 | 30 | 388.998 | 550.000 |
| 30 | BOTS | 06 | 27 | 30 | 60.000 | 120.000 |
| 30 | BOT | 06 | 27 | 30 | 120.000 | 172.070 |
| 30 | FR6BB | 06 | 27 | 30 | 172.070 | 178.737 |
| 30 | FR6F | 06 | 27 | 30 | 178.737 | 318.437 |
| 30 | FR6FT | 06 | 27 | 30 | 318.437 | 334.312 |
| 30 | FR6T | 06 | 27 | 30 | 334.312 | 338.998 |
| 30 | TOPS | 06 | 27 | 30 | 338.998 | 388.998 |
|  |  |  |  |  |  |  |
| 30 | OREF | 07 |  |  | 0.0 | 60.000 |
| 30 | OREF | 07 |  | 388.998 | 550.000 |  |
| 30 | BOTS | 07 |  | 60.000 | 120.000 |  |
| 30 | BOT | 07 |  | 120.000 | 172.070 |  |
| 30 | R7BB | 07 |  | 172.070 | 178.737 |  |
| 30 | R7F | 07 |  | 178.737 | 318.437 |  |
| 30 | R7FT | 07 |  | 318.437 | 334.312 |  |
| 30 | R7T | 07 |  | 334.312 | 338.998 |  |
| 30 | TOPS | 07 |  | 338.998 | 388.998 |  |


| 30 | OREF | 07 | 1 | 6 | 0.0 | 60.000 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | OREF | 07 | 1 | 6 | 388.998 | 550.000 |
| 30 | BOTS | 07 | 1 | 6 | 60.000 | 120.000 |
| 30 | BOT | 07 | 1 | 6 | 120.000 | 172.070 |
| 30 | R7BB | 07 | 1 | 6 | 172.070 | 178.737 |
| 30 | R7F | 07 | 1 | 6 | 178.737 | 318.437 |
| 30 | R7FT | 07 | 1 | 6 | 318.437 | 334.312 |
| 30 | R7T | 07 | 1 | 6 | 334.312 | 338.998 |
| 30 | TOPS | 07 | 1 | 6 | 338.998 | 388.998 |
|  |  |  |  |  |  |  |
| 30 | OREF | 07 | 7 | 7 | 0.0 | 60.000 |
| 30 | OREF | 07 | 7 | 7 | 388.998 | 550.000 |
| 30 | BOTS | 07 | 7 | 7 | 60.000 | 120.000 |
| 30 | BOT | 07 | 7 | 7 | 120.000 | 172.070 |
| 30 | R7BB | 07 | 7 | 7 | 172.070 | 178.737 |
| 30 | R7DET | 07 | 7 | 7 | 178.737 | 318.437 |
| 30 | R7FT | 07 | 7 | 7 | 318.437 | 334.312 |
| 30 | R7T | 07 | 7 | 7 | 334.312 | 338.998 |
| 30 | TOPS | 07 | 7 | 7 | 338.998 | 388.998 |
| 3 |  |  |  |  |  |  |
| 30 | OREF | 07 | 8 | 28 | 0.0 | 60.000 |
| 30 | OREF | 07 | 8 | 28 | 388.998 | 550.000 |


| 30 | BOTS | 07 | 8 | 28 | 60.000 | 120.000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | BOT | 07 | 8 | 28 | 120.000 | 172.070 |
| 30 | R7BB | 07 | 8 | 28 | 172.070 | 178.737 |
| 30 | R7F | 07 | $8 \quad 2$ | 28 | 178.737 | 318.437 |
| 30 | R7FT | 07 | 8 | 28 | 318.437 | 334.312 |
| 30 | R7T | 07 | 8 | 28 | 334.312 | 338.998 |
| 30 | TOPS | 07 | 8 | 28 | 338.998 | 388.998 |
| 30 | OREF | 07 | 29 | 29 | 0.0 | 60.000 |
| 30 | OREF | 07 | 29 | 29 | 388.998 | 8550.000 |
| 30 | BOTS | 07 | 29 | 29 | 60.000 | 120.000 |
| 30 | BOT | 07 | 29 | 29 | 120.000 | 172.070 |
| 30 | R7BB | 07 | 29 | 29 | 172.070 | 178.737 |
| 30 | SOURB | - 07 | 29 | 29 | 9178.737 | $37 \quad 234.458$ |
| 30 | SOURC1 | 107 | $7 \quad 29$ | 9 29 | $29 \quad 234.458$ | 270.577 |
| 30 | SOURT | 07 | 29 | 29 | 9270.577 | $77 \quad 318.437$ |
| 30 | R7FT | 07 | 29 | 29 | 318.437 | 334.312 |
| 30 | R7T | 07 | 29 | 29 | 334.312 | 338.998 |
| 30 | TOPS | 07 | 29 | 29 | 338.998 | 388.998 |
| 30 | OREF | 07 | 30 | 36 | 0.0 | 60.000 |
| 30 | OREF | 07 |  | 36 | 388.998 | 8550.000 |
| 30 | BOTS | 07 | 30 | 36 | 60.000 | 120.000 |
| 30 | BOT | 07 | 30 | 36 | 120.000 | 172.070 |
| 30 | R7BB | 07 | 30 | 36 | 172.070 | - 178.737 |
| 30 | R7F | 07 | 30 | 36 | 178.737 | 318.437 |
| 30 | R7FT | 07 | 30 | 36 | 318.437 | 334.312 |
| 30 | R7T | 07 | 30 | 36 | 334.312 | 338.998 |
| 30 | TOPS | 07 | 30 | 36 | 338.998 | - 388.998 |
| OUTER BLANKET REGION |  |  |  |  |  |  |
| 30 | OREF8 | 08 |  |  | $0.0 \quad 60$ | 60.000 |
| 30 | OREF8 | 08 |  |  | 388.998 | 550.000 |
| 30 | BOTS | 08 |  |  | $60.000 \quad 1$ | 120.000 |
| 30 | BOT | 08 |  |  | $120.000 \quad 1$ | 172.070 |
| 30 | R8BB | 08 |  |  | 172.070 | 178.737 |
| 30 | R8F | 08 |  |  | 78.737318 | 318.437 |
| 30 | R8FT | 08 |  |  | 318.437 | 334.312 |
| 30 | R8T | 08 |  |  | 334.312338 | 338.998 |
| 30 | TOPS | 08 |  |  | 338.998 | 388.998 |
| 30 | OREF9 | 09 |  |  | 0.060 | 60.000 |
| 30 | OREF9 | 09 |  |  | 388.998 | 550.000 |
| 30 | BOTS | 09 |  |  | $60.000 \quad 1$ | 120.000 |
| 30 | BOT | 09 |  |  | $120.000 \quad 17$ | 172.070 |
| 30 | R9BB | 09 |  |  | 172.070 | 178.737 |
| 30 | R9F | 09 |  |  | 78.737318 | 318.437 |
| 30 | R9FT | 09 |  |  | 318.437 | 334.312 |
| 30 | R9T | 09 |  |  | 334.312 338 | 338.998 |
| 30 | TOPS | 09 |  |  | 338.998 | 388.998 |
| 30 | OREF10 | 10 |  |  | 0.06 | 60.000 |
| 30 | OREF10 | 10 |  |  | 388.998 | 550.000 |
| 30 | BOTS | 10 |  |  | 60.0001 | 120.000 |
| 30 | BOT | 10 |  |  | 120.0001 | 172.070 |


| 30 | R10BB | 10 |  |  | 172.070 | 178.737 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | R10F | 10 |  |  | 178.7373 | 318.437 |
| 30 | R10FT | 10 |  |  | 318.437 | 334.312 |
| 30 | R10T | 10 |  |  | 334.3123 | 338.998 |
| 30 | TOPS | 10 |  |  | 338.998 | 388.998 |
| 30 | OREF11 | 11 |  |  | 0.06 | 60.000 |
| 30 | OREF11 | 11 |  |  | 388.998 | 550.000 |
| 30 | BOTS | 11 |  | 23 | 60.000 | 120.000 |
| 30 | BOT | 11 |  | 23 | 120.000 | 172.070 |
| 30 | R11BB | 11 | 1 | 23 | 172.070 | 178.737 |
| 30 | R11F | 11 |  | 23 | 178.737 | 318.437 |
| 30 | R11FT | 11 | 1 | 23 | 318.437 | 334.312 |
| 30 | R11T | 11 | 1 | 23 | 334.312 | 338.998 |
| 30 | TOPS | 11 | 1 | 23 | 338.998 | 388.998 |
| 30 | BOTS | 11 | 24 | 24 | 60.000 | 120.000 |
| 30 | BOT | 11 | 24 | 24 | 120.000 | 172.070 |
| 30 | R11BB | 11 | 24 | 24 | 172.070 | - 178.737 |
| 30 | R11DET | 11 | 24 | 24 | $4 \quad 178.737$ | 7318.437 |
| 30 | R11FT | 11 | 24 | 24 | 318.437 | 334.312 |
| 30 | R11T | 11 | 24 | 24 | 334.312 | 338.998 |
| 30 | TOPS | 11 |  | 24 | 338.998 | 388.998 |
| 30 | BOTS | 11 | 25 | 60 | 60.000 | 120.000 |
| 30 | BOT | 11 | 25 | 60 | 120.000 | 172.070 |
| 30 | R11BB | 11 | 25 | 60 | - 172.070 | - 178.737 |
| 30 | R11F | 11 | 25 | 60 | 178.737 | 318.437 |
| 30 | R11FT | 11 | 25 | 60 | 318.437 | 334.312 |
| 30 | R11T | 11 | 25 | 60 | 334.312 | 338.998 |
| 30 | TOPS | 11 | 25 | 60 | 338.998 | 388.998 |
| 30 | OREF12 | 12 |  |  | 0.06 | 60.000 |
| 30 | OREF12 | 12 |  |  | 388.998 | 550.000 |
| 30 | BOTS | 12 |  |  | 60.0001 | 120.000 |
| 30 | BOT | 12 |  |  | 120.000 | 172.070 |
| 30 | R12BB | 12 |  |  | 172.070 | 178.737 |
| 30 | R12F | 12 |  |  | 178.7373 | 318.437 |
| 30 | R12FT | 12 |  |  | 318.437 | 334.312 |
| 30 | R12T | 12 |  |  | 334.312 | 338.998 |
| 30 | TOPS | 12 |  |  | 338.998 | 388.998 |
| 30 | OREF13 | 13 |  |  | 0.060 | 60.000 |
| 30 | OREF13 | 13 |  |  | 388.998 | 550.000 |
| 30 | BOTS | 13 | 1 | 17 | 60.000 | 120.000 |
| 30 | BOT | 13 | 1 | 17 | 120.000 | 172.070 |
| 30 | R13BB | 13 | 1 | 17 | 172.070 | 178.737 |
| 30 | R13F | 13 | 1 | 17 | 178.737 | 318.437 |
| 30 | R13FT | 13 | 1 | 17 | 318.437 | 334.312 |
| 30 | R13T | 13 | 1 | 17 | 334.312 | 338.998 |
| 30 | TOPS | 13 | 1 | 17 | 338.998 | 388.998 |
| 30 | BOTS | 13 | 18 | 18 | 60.000 | 120.000 |
| 30 | BOT | 13 | 18 | 18 | 120.000 | 172.070 |
| 30 | R13BB | 13 | 18 | 18 | 172.070 | -178.737 |
| 30 | R13DET | 13 | 18 | 18 | $8 \quad 178.737$ | 37318.437 |


| 30 | R13FT | 13 | 18 | 18 | 318.437 | 334.312 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | R13T | 13 | 18 | 18 | 334.312 | 338.998 |
| 30 | TOPS | 13 | 18 | 18 | 338.998 | 388.998 |
|  |  |  |  |  |  |  |
| 30 | BOTS | 13 | 19 | 72 | 60.000 | 120.000 |
| 30 | BOT | 13 | 19 | 72 | 120.000 | 172.070 |
| 30 | R13BB | 13 | 19 | 72 | 172.070 | 178.737 |
| 30 | R13F | 13 | 19 | 72 | 178.737 | 318.437 |
| 30 | R13FT | 13 | 19 | 72 | 318.437 | 334.312 |
| 30 | R13T | 13 | 19 | 72 | 334.312 | 338.998 |
| 30 | TOPS | 13 | 19 | 72 | 338.998 | 388.998 |


| 30 | OREF14 | 14 |  |  | 0.0 | 60.000 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | OREF14 | 14 |  | 388.998 | 550.000 |  |
| 30 | BOTS | 14 |  |  | 60.000 | 120.000 |
| 30 | BOT | 14 |  |  | 120.000 | 172.070 |
| 30 | R14BB | 14 |  |  | 172.070 | 178.737 |
| 30 | R14F | 14 |  |  | 178.737 | 318.437 |
| 30 | R14FT | 14 |  |  | 318.437 | 334.312 |
| 30 | R14T | 14 |  |  | 334.312 | 338.998 |
| 30 | TOPS | 14 |  |  | 338.998 | 388.998 |
|  |  |  |  |  |  |  |
| 30 | OREF15 | 15 |  |  | 0.0 | 60.000 |
| 30 | OREF15 | 15 |  |  | 388.998 | 550.000 |
| 30 | EMPT | 15 | 1 | 2 | 60.000 | 388.998 |
| 30 | BOTS | 15 | 3 | 13 | 60.000 | 120.000 |
| 30 | BOT | 15 | 3 | 13 | 120.000 | 172.070 |
| 30 | R15BB | 15 | 3 | 13 | 172.070 | 178.737 |
| 30 | R15F | 15 | 3 | 13 | 178.737 | 318.437 |
| 30 | R15FT | 15 | 3 | 13 | 318.437 | 334.312 |
| 30 | R15T | 15 | 3 | 13 | 334.312 | 338.998 |
| 30 | TOPS | 15 | 3 | 13 | 338.998 | 388.998 |
| 30 | EMPT | 15 | 14 | 16 | 60.000 | 388.998 |
| 30 | BOTS | 15 | 17 | 27 | 60.000 | 120.000 |
| 30 | BOT | 15 | 17 | 27 | 120.000 | 172.070 |
| 30 | R15BB | 15 | 17 | 27 | 172.070 | 178.737 |
| 30 | R15F | 15 | 17 | 27 | 178.737 | 318.437 |
| 30 | R15FT | 15 | 17 | 27 | 318.437 | 334.312 |
| 30 | R15T | 15 | 17 | 27 | 334.312 | 338.998 |
| 30 | TOPS | 15 | 17 | 27 | 338.998 | 388.998 |
| 30 | EMPT | 15 | 28 | 30 | 60.000 | 388.998 |
| 30 | BOTS | 15 | 31 | 41 | 60.000 | 120.000 |
| 30 | BOT | 15 | 31 | 41 | 120.000 | 172.070 |
| 30 | R15BB | 15 | 31 | 41 | 172.070 | 178.737 |
| 30 | R15F | 15 | 31 | 41 | 178.737 | 318.437 |
| 30 | R15FT | 15 | 31 | 41 | 318.437 | 334.312 |
| 30 | R15T | 15 | 31 | 41 | 334.312 | 338.998 |
| 30 | TOPS | 15 | 31 | 41 | 338.998 | 388.998 |
| 30 | EMPT | 15 | 42 | 44 | 60.000 | 388.998 |
| 30 | BOTS | 15 | 45 | 55 | 60.000 | 120.000 |
| 30 | BOT | 15 | 45 | 55 | 120.000 | 172.070 |
| 30 | R15BB | 15 | 45 | 55 | 172.070 | 178.737 |
| 30 | R15F | 15 | 45 | 55 | 178.737 | 318.437 |
|  |  |  |  |  |  |  |


| 30 | R15FT | 15 | 45 | 55 | 318.437 | 334.312 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | R15T | 15 | 45 | 55 | 334.312 | 338.998 |
| 30 | TOPS | 15 | 45 | 55 | 338.998 | 388.998 |
| 30 | EMPT | 15 | 56 | 58 | 60.000 | 388.998 |
| 30 | BOTS | 15 | 59 | 69 | 60.000 | 120.000 |
| 30 | BOT | 15 | 59 | 69 | 120.000 | 172.070 |
| 30 | R15BB | 15 | 59 | 69 | 172.070 | 178.737 |
| 30 | R15F | 15 | 59 | 69 | 178.737 | 318.437 |
| 30 | R15FT | 15 | 59 | 69 | 318.437 | 334.312 |
| 30 | R15T | 15 | 59 | 69 | 334.312 | 338.998 |
| 30 | TOPS | 15 | 59 | 69 | 338.998 | 388.998 |
| 30 | EMPT | 15 | 70 | 72 | 60.000 | 388.998 |
| 30 | BOTS | 15 | 73 | 83 | 60.000 | 120.000 |
| 30 | BOT | 15 | 73 | 83 | 120.000 | 172.070 |
| 30 | R15BB | 15 | 73 | 83 | 172.070 | 178.737 |
| 30 | R15F | 15 | 73 | 83 | 178.737 | 318.437 |
| 30 | R15FT | 15 | 73 | 83 | 318.437 | 334.312 |
| 30 | R15T | 15 | 73 | 83 | 334.312 | 338.998 |
| 30 | TOPS | 15 | 73 | 83 | 338.998 | 388.998 |
| 30 | EMPT | 15 | 84 | 84 | 60.000 | 388.998 |
| 30 | OREF16 | 16 |  |  | 0.0 | 0.000 |
| 30 | OREF16 | 16 |  |  | 388.998 | 550.000 |
| 30 | EMPT | 16 | 1 | 6 | 60.000 | 388.998 |
| 30 | BOTS | 16 | 7 | 10 | 60.000 | 120.000 |
| 30 | BOT | 16 | 7 | 10 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 7 | 10 | 172.070 | 178.737 |
| 30 | R16F | 16 | 7 | 10 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 7 | 10 | 318.437 | 334.312 |
| 30 | R16T | 16 | 7 | 10 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 7 | 10 | 338.998 | 388.998 |
| 30 | EMPT | 16 | 11 | 21 | 60.000 | 388.998 |
| 30 | BOTS | 16 | 22 | 25 | 60.000 | 120.000 |
| 30 | BOT | 16 | 22 | 25 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 22 | 25 | 172.070 | 178.737 |
| 30 | R16F | 16 | 22 | 25 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 22 | 25 | 318.437 | 334.312 |
| 30 | R16T | 16 | 22 | 25 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 22 | 25 | 338.998 | 388.998 |
| 30 | EMPT | 16 | 26 | 36 | 60.000 | 388.998 |
| 30 | BOTS | 16 | 37 | 40 | 60.000 | 120.000 |
| 30 | BOT | 16 | 37 | 40 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 37 | 40 | 172.070 | ) 178.737 |
| 30 | R16F | 16 | 37 | 40 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 37 | 40 | 318.437 | 334.312 |
| 30 | R16T | 16 | 37 | 40 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 37 | 40 | 338.998 | 388.998 |
| 30 | EMPT | 16 | 41 | 51 | 60.000 | 388.998 |
| 30 | BOTS | 16 | 52 | 55 | 60.000 | 120.000 |
| 30 | BOT | 16 | 52 | 55 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 52 | 55 | 172.070 | ) 178.737 |
| 30 | R16F | 16 | 52 | 55 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 52 | 55 | 318.437 | 334.312 |
| 30 | R16T | 16 | 52 | 55 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 52 | 55 | 338.998 | 388.998 |
| 30 | EMPT | 16 | 56 | 66 | 60.000 | 388.998 |


| 30 | BOTS | 16 | 67 | 70 | 60.000 | 120.000 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | BOT | 16 | 67 | 70 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 67 | 70 | 172.070 | 178.737 |
| 30 | R16F | 16 | 67 | 70 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 67 | 70 | 318.437 | 334.312 |
| 30 | R16T | 16 | 67 | 70 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 67 | 70 | 338.998 | 388.998 |
| 30 | EMPT | 16 | 71 | 81 | 60.000 | 388.998 |
| 30 | BOTS | 16 | 71 | 81 | 60.000 | 120.000 |
| 30 | BOT | 16 | 71 | 81 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 71 | 81 | 172.070 | 178.737 |
| 30 | R16F | 16 | 71 | 81 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 71 | 81 | 318.437 | 334.312 |
| 30 | R16T | 16 | 71 | 81 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 71 | 81 | 338.998 | 388.998 |
| 30 | EMPT | 16 | 82 | 85 | 60.000 | 388.998 |
| 30 | BOTS | 16 | 86 | 90 | 60.000 | 120.000 |
| 30 | BOT | 16 | 86 | 90 | 120.000 | 172.070 |
| 30 | R16BB | 16 | 86 | 90 | 172.070 | 178.737 |
| 30 | R16F | 16 | 86 | 90 | 178.737 | 318.437 |
| 30 | R16FT | 16 | 86 | 90 | 318.437 | 334.312 |
| 30 | R16T | 16 | 86 | 90 | 334.312 | 338.998 |
| 30 | TOPS | 16 | 86 | 90 | 338.998 | 388.998 |
| 30 | ORE17 | 17 |  |  | 0.0 | 550.000 |
| 30 | OREF18 | 18 |  | 0.0 | 550.000 |  |
| 30 | ORE |  |  | 0.0 | 550.000 |  |
| 30 | OREF19 | 19 |  |  | 0.0 | 550.000 |
| 30 | OREF20 | 20 |  |  | 0.0 | 550.000 |
| 30 | OREF21 | 21 |  |  | 0.0 | 550.000 |
| 30 | OREF22 | 22 |  |  | 0.0 | 550.000 |
| 30 | OREF23 | 23 |  |  | 0.0 | 550.000 |
| 30 | OREF24 | 24 |  |  | 0.0 | 550.000 |
| 30 | OREF25 | 25 |  |  |  |  |

